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# Gravity Law without Universalism is solving many tasks

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**Abstract** My MOND proposal includes General Relativity as a special case, i.e. I have effects of General Relativity in many areas of spacetime. I argue that my proposal can describe Dark Matter as well if one understands the modification of gravity as a tensor field  $X^{\mu\nu}(t, x, y, z)$  in the Einstein equations, i.e. as an additional mathematical parameter filling the Universe without correspondence to new particles. Notably, there are many different fields in nature, e.g. the Higgs field, the inflaton field, and the temperature distribution field  $T(t, x, y, z)$ . My testable prediction that they will never find weakly interacting Dark Matter particles is well-realized up to today; therefore, Popper's falsifiability criterion is satisfied because the underground detectors could report the signal. On the other hand, the testable proof would be the indirect discovery of the sterile neutrino. As it does not interact with visible matter even weakly, it is an example of  $X^{\mu\nu}$ . This justified theory, applied to key problems of Physics, provides satisfactory answers.

**Keywords** Dark Matter; Dark Energy; Alternative gravity theories; Geodesic; Cosmological Constant Problem; Information Paradox

## 1 And because mistakes and fakes shall abound, the way of truth will be evil spoken of

*This section can be removed from the paper on request of the referee. It is not meant as a proposal to modify the peer-review process, but as an argument for the referee to use goodwill.*

The goal “to find mistakes” could be a bad attitude. The final goal should be to enjoy reading the publication. If flaws are seen, they must be reported. However, this report should be given without any laughs and sadistic enjoyment. Instead, the flaws should be reported with some sadness.

The psychologists have conducted a social experiment: they told the probants that the man on the photo is a serial killer. The probants testified that he is looking like one. The next day they told another group of probants that the man on the same photo is an American national hero; these probants have confirmed his heroic look.

In conclusion, having the “mistakes desire” as your default position while reading the manuscript of an unknown author increases the chances for the paper to be unjustly rejected. The scientific skepticism should be the readiness to deal with mistakes, but not the expectation – by desire – to find them.

Why do I ask as an author for detailed reports from the referee system? The referee must convince me that I have done mistakes. Otherwise, I would not accept them. Yes, it seems like living in an “utopian” perfect world. But I cannot repent a hypothetical mistake. I can only repent if the mistake is demonstrated to me and I am convinced that it is not the usual fake-news, trolling or bullying. This research principle is my personal “guiding star” during my quest for the objective truth. As an example, the absolute majority of scientists have accepted the proof for Goldbach's weak conjecture, but not all of the scientists have accepted it yet, mainly because it is not published in a journal. <sup>1</sup>

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<sup>1</sup>Harald A. Helfgott, “The ternary Goldbach conjecture is true”, arXiv:1312.7748 [math.NT].

Therefore, one needs to have personal convictions and opinions to move forward.<sup>2</sup>

To navigate in Science, you need to have a personal point of view and convictions you should not rush to abandon. Otherwise, you will soon be disoriented. Only then you will realize the objective truth. That is the subjective search for the objective truth because you are choosing what is right and what is not.

## 2 Introduction

What is the nature of dark matter? Is it a particle, or do the phenomena attributed to dark matter actually require a modification of the laws of gravity? In this first publication in a series of papers I deal with this question without applying mathematical tools. Nevertheless, all my points are backed up by evidence. The next two publications entitled “Broken Geodesics and Dark Matter” and “Energy Localization Problem points out the vanishing of matter in the First Order Deviation Equation” are highly mathematical applications of the theory described in this note. My approach is not in contradiction with the standard  $\Lambda$ CDM cosmology but fixes possible problems of it (Chen 2019).

Modified Newtonian dynamics (MOND) is a hypothesis that proposes a modification of Newton’s laws to account for observed properties of galaxies. It is an alternative to the hypothesis of dark matter in terms of explaining why galaxies do not appear to obey the currently understood laws of physics. Created in 1982 and first published in 1983 by the Israel physicist Mordehai Milgrom (Milgrom 1983), the hypothesis’ original motivation was to explain why the velocities of stars in galaxies were observed to be larger than those expected by using Newtonian mechanics.

MOND is an example of a class of theories known as modified gravity, and it is an alternative to the hypothesis that the dynamics of galaxies are determined by massive, invisible dark matter halos. Since Milgrom’s original proposal, MOND has successfully predicted a variety of galactic phenomena that are difficult to understand from a dark matter perspective (Banik 2018). However, MOND and its generalisations do not adequately account for observed properties of galaxy clusters, and no satisfactory cosmological model has been constructed from the hypothesis.

The accurate measurement of the speed of gravitational waves compared to the speed of light in 2017 ruled out many theories which used modified gravity to avoid dark matter (Boran 2018). However, according to the same study neither Milgrom’s bi-metric formulation of MOND nor nonlocal MOND are ruled out.

## 3 Common feature of MOND proposals

Newton’s law of universal gravitation usually states that every particle attracts every other particle in the universe with a force which is directly proportional to the product of their masses and inversely proportional to the square of the distance between their centers. This is a general physical law derived from empirical observations by what Isaac Newton called inductive reasoning (Newton 1729).

The common feature of all MOND proposals is this universalism. Given the energy-momentum tensor for “visible” (e.g., baryonic) matter, one perfectly determines Dark Matter. However, that seems to be not true because galaxies without Dark Matter are discovered (Dokkum 2018). In contrast to this, I introduce a non-universal law of gravitation in Eq. (2). According to this, there are places and times in the universe where the gravitational force cannot be calculated just from the properties of visible matter. To fix the problems of MOND, I suggest to include a tensor field of Dark Matter.

## 4 How to modify gravity

A general expression for modified gravity can be written as

$$G^{*\mu\nu} = 8\pi T^{\mu\nu}, \quad (1)$$

where the left hand side is the modified Einstein tensor.  $T^{\mu\nu}$  is the energy-momentum tensor of visible matter. Without loss of generality one can rewrite Eq. (1) using the definition  $8\pi X^{\mu\nu} = G^{\mu\nu} - G^{*\mu\nu}$ ,

$$G^{\mu\nu} = 8\pi (T^{\mu\nu} + X^{\mu\nu}), \quad (2)$$

where the unmodified Einstein tensor is on the left hand side. In the following I call  $X^{\mu\nu}$  a virtual term, in particular Virtual Matter. This term cannot be detected in particle detectors, as it is not visible matter but rather a pure mathematical modification of Einstein’s equations. In case the covariant divergence  $X^{\mu\nu}_{;\nu}$  vanishes, we will call it Dark Matter. In this sense, Dark Energy is a class of Dark Matter because  $(\Lambda g^{\mu\nu})_{;\nu} = 0$ .

<sup>2</sup>Massimiliano Proietti *et. al.*, Experimental test of local observer-independence, *Science Advances* 5(9), eaaw9832 (2019), arXiv:1902.05080 [quant-ph]; Ian T. Durham, Observer-independence in the presence of a horizon, arXiv:1902.09028 [quant-ph]

My proposal is to allow the 10 independent functions  $X^{\mu\nu} = X^{\mu\nu}(t, x, y, z)$  not to be universal, i.e. being not always the most popular expression of Dark Matter (which is dust-like tensor  $X_{\nu}^{\mu} = \text{diag}(-\rho, 0, 0, 0)$ ), but different in any given task and problem. What determines the shape of  $X^{\mu\nu}$ ? Is it theoretical physics or experiment/observation? My answer is, that it is both, as e.g. in Section IV the introduction of  $X^{\mu\nu}$  turns out to be a solution to particular theoretical problems. Therefore, one can not blame my proposal for having no predictive power – despite the fact that the absolute generality of Eq. (2) fits any possible experiment or observation.

## 5 Evidences of the necessity of $X^{\mu\nu}$ for fixing problems

### 5.1 Fixing singularities

Using known facts from General Relativity, it is indeed possible and easy to solve the mystery. Any singularity is simply a mathematical blow up of the theory of Relativity. To fix this and to make the theory physical rather than mathematical, I am using a virtual term  $\psi(r)$  in the Schwarzschild Black Hole metrics,

$$ds^2 = -\left(1 - \frac{2M}{r + \psi(r)}\right) dt^2 + \frac{dr^2}{1 - \frac{2M}{r + \psi(r)}} + r^2 d\Omega^2, \quad (3)$$

where  $\psi(r > 2M) = 0$ ,  $\psi(r \leq 2M) = \epsilon(2M - r)$  for  $0 \leq r < \infty$  and small  $\epsilon > 0$ .

The tensor  $X^{\mu\nu}$  can be calculated from Eqs. (2) and (3) for  $T^{\mu\nu} = 0$ . The demand to fulfil the “energy conditions” (weak, strong, and others) is not applicable to the virtual matter  $X^{\mu\nu}$ , as it is not subject to measurements. So one would not measure a negative energy. Notably, the known concepts of “phantom fields” (Singh 2003) and “exotic matter” (Ivanov 2009; Morris 1988) have problems with energy conditions, but considering them as the examples of Virtual Matter, they have no such problems. By the way, any possible instability of my MOND proposal is simply removed by properly chosen variations of the arbitrary virtual term  $X^{\mu\nu}$ .

### 5.2 Fixing abrupt geodesics

If one releases a particle in Kerr, Kerr–Newman, or Reissner–Nordström spacetime with zero initial velocity  $u^r = u^\theta = u^\phi = 0$  (in case of photon  $u^\theta = u^\phi = 0$ ,  $u^r < 0$ ), it will reach an abrupt end of the trajectory at the radius  $r = r_m > 0$ , because there is  $(u^r)^2 < 0$  for  $r < r_m$ . The curvature singularity is at  $r = 0$ . Note that

in case of a motion inside the equatorial plane  $\theta = \pi/2$  the abrupt end geodesics are present for Kerr–Newman and Reissner–Nordström spacetimes. The abrupt end of geodesics means the vanishing of matter.

Notably, Einstein’s vision of a steady-state universe theory contains the “formation of matter from empty space”, so that the density of matter in the expanding universe is kept constant. But it turned out that Einstein’s equations are violated by such an assumption (O’Raifeartaigh 2014). Indeed, the appearance of matter in “forward time” is equivalent to the vanishing of matter in “backwards time”. If so, one needs to use a properly chosen virtual term  $X^{\mu\nu}$  to revisit the Einstein’s proposal.

The details are found in Ref. (Martila 2019) which uses velocity expressions from Ref. (Lightman 1975). An evidence is presented in Appendix below.

### 5.3 Fixing the Cosmology Constant Problem

In cosmology, the “cosmological constant problem” or “vacuum catastrophe” is the disagreement in non-modified General Relativity (Einstein 1916) between the small value of spacetime curvature (taken at global scale) and the theoretical large value of the zero-point energy suggested by quantum field theories. Depending on the “Planck energy cutoff” and other factors, the discrepancy is as high as 120 orders of magnitude, a state of affairs described by physicists as “the largest discrepancy between theory and experiment in all of science” and “the worst theoretical prediction in the history of physics.” (Adler 1995)

In my MOND proposal the “fixing” of this problem can be conducted by using the fixing of the spacetime metric tensor via  $X^{\mu\nu} \neq 0$ ; hereby the friction-free inertial motion of visible matter inside the “sea” of (invisible) virtual particles of vacuum is explained in a most natural and easy way, because the virtual particles can be seen as an example of my Virtual Matter. It is an amazing historic coincidence that the virtual particles and my Virtual Matter concept both contain the word “virtual”.

Here and in the following, “fixing” of spacetime means that we start by postulating the metric tensor  $g_{\mu\nu}$ , after that finding the behaviour of the visible matter in a given spacetime area (e.g. the motion of the test-particle below). Note that the “fixed” metric can be non-stationary. One indeed can notice that although we are used to read Eq.(1) from right to left (i.e. given the tensor  $T^{\mu\nu}$  one finds the metric tensor by solving the differential equations), one can perform the following trick: starting with some considerations for  $g_{\mu\nu}$  and taking the partial derivatives one easily finds the Einstein tensor  $G^{\mu\nu}$ , then given some  $X^{\mu\nu}$  one finds the parameters inside the  $T^{\mu\nu}$ .

### 5.3.1 Occam's razor and Dark Energy

Occam's razor is the problem-solving principle that states that "Entities should not be multiplied without necessity." (Schaffer 2015) The idea is attributed to English Franciscan friar William of Ockham (1287–1347), a scholastic philosopher and theologian who used a preference for simplicity to defend the idea of divine miracles. It is sometimes paraphrased by a statement like "the simplest solution is most likely the right one."

According to this principle, if the influence of vacuum energy is that much reduced (more than  $10^{120}$  times), the most simple and natural theory is the complete absence of such an influence (due to a counterparting tensor  $X^{\mu\nu}$ ). In such case we would be lacking of an undisputed proof for the Dark Energy. Amazingly, there are new papers which put the existence of Dark Energy in doubt (Kang 2020).

### 5.4 Fixing the test-particle formalism

The known geodesic equation  $u^\mu_{;\nu} u^\nu = 0$  of a test-particle motion silently assumes that the background spacetime is fixed, i.e. that there is no backreaction from high-speed (e.g. near Black Holes) geodesic motion on the spacetime.

The absence of a backreaction is only possible if  $X^{\mu\nu} \neq 0$  is present in Eq. (2). This would be the simplest solution for the topic of backreaction, while other solutions have major mathematical complications with accounting for the gravitational backreaction, e.g. in Refs. (Hawking 1974).

### 5.5 Fixing the static universe

I am talking not about the real Universe (the one we are living in), but about an imaginable one, which is constructed from the known laws of nature.

It is known that the pressure in the perfect fluid model allows us to have a static drop of fluid in empty spacetime. It is expected that pressure as the resistance of matter counterparts gravity, and so a static universe filled with a perfect fluid should be allowed. Hereby, in case of the "flat Friedmann universe" metric,  $X^{\mu\nu} = -T^{\mu\nu} \neq 0$  can be necessary.

It is interesting that while trying to construct the static universe (Einstein 1917), Albert Einstein found an example for a non-zero  $8\pi X^{\mu\nu} = -\Lambda g^{\mu\nu} \neq 0$ , naming it later the "biggest blunder" (Bodanis 2016) of his life without even realizing the entire potential and usefulness of this discovery (e.g. the possibility of interstellar travel (Morris 1988)).

## 6 Conclusions

Increasingly, we see phenomena that do not lead to the emergence of new experimentally confirmed theories or to the update of old theories acceptable to all scientists; an example is the (yet) futile search for Quantum Gravity and the Theory of Everything in an attempt to explain the cosmological singularity and Black Holes. It should be expected then that some known phenomena (like perhaps in Ref. (Wilczynska 2020)) are explainable solely by the insertions of virtual terms. These are mathematical insertions into the equations and laws of nature which can be made not necessarily from fundamental premises (like the principle of least action) but "by hand" in order to fit the theory under observation. An example for such insertions are Dark Matter and Dark Energy. Therefore, these cannot be directly detected, but it is possible to measure their effect on nature. As a prime example, the Dark Matter anomaly has acted on the space-time grid in such an way that it created an additional force of attraction of stars to the center of their galaxy. By the way, the proton radius measured by many experimenters was different in different years. This riddle did not find yet a solution (Karr 2019). Personally, I would solve this problem with a virtual insertion  $\Psi$  into the radius value,  $r = R + \Psi$ .

The proton radius puzzle is an unanswered problem in physics relating to the size of the proton (Krauth 2017). Historically the proton charge radius was measured by two independent methods which converged to a value of about 0.877 femtometres. This value was challenged by an 2010 experiment using a third method which produced a radius about 4% smaller than this, at 0.842 femtometres (Pohl 2010). New experimental results reported in the fall of 2019 agree with the smaller measurement, and it has been proposed that the puzzle is now solved (Hammer 2019), though this opinion is not yet common (Karr 2019).

### 6.1 Fixing ultra-high energy cosmic rays

Another example is the (yet) futile search for the origin of ultra-high energy cosmic rays (Palladino 2020). Picking up as "virtual term", a specific initial condition (based on the observed spectrum) for the rays is the only available way (at least for today) to solve this problem.

### 6.2 Fixing the non-vanishing neutrino mass

The next example are the ugly attempts to upgrade the Standard Model to allow for a non-vanishing neutrino mass. It is logical then that the neutrino masses are the

sum of the Standard Model suggestion and the virtual insertion:  $m_{\text{reality}} = m_{SM} + m_{\Psi} = m_{\Psi}$ . In this case we do not need to upgrade the Standard Model at all, because any upgrade can lead us along the wrong path. Independent of this, each scientist is of course free to look for an upgrade of the Standard Model, as we are not under the inquisition.

### 6.3 Fixing to missing antimatter

A virtual term at the initial conditions fixes the “missing antimatter paradox”, for Dr. Christian Smorra comments the paradox as “All of our observations find a complete symmetry between matter and antimatter, which is why the universe should not actually exist. An asymmetry must exist here somewhere but we simply do not understand where the difference is. What is the source of the symmetry break?” (Smorra 2017)

### 6.4 Fixing the wave function collapse of the Copenhagen Interpretation of Quantum Mechanics

In case the wave function collapse, Einstein’s equations are violated and Quantum Gravity seems to be needed (Hossenfelder 2020). Instead, my virtual matter fixes any these problems.

### 6.5 Beauty and simplicity of my MOND proposal

Despite of a recently published book by Sabine Hossenfelder (Hossenfelder 2018) which blames the feeling of beauty for creating problems, one can show that my MOND proposal is so much beautiful that it could satisfy even the highest standards of scientific beauty posed by Albert Einstein.

By calling  $X^{\mu\nu}$  matter (invisible matter) the author restores Einstein’s original idea (Einstein 1916). For the scientific community there is no need to modify General Relativity if one accepts the existence of invisible (Virtual) matter. The “sterile neutrino” does not interact with visible matter even “weakly”. As the sterile neutrino cannot be directly detected by neutrino detectors, it can be regarded as a theoretical example of my invisible matter concept. Already the confidence level of  $6\sigma$  is reported in Ref. (Aguilar-Arevalo 2018).

Matter is defined to be invisible if it does not interact with visible matter (e.g. with baryonic matter). Examples of invisible matter are sterile neutrinos. Hereby, gravitational interaction cannot be called a true interaction, because according to Albert Einstein gravity is not a force. Reality works on proper definitions and on the correct use of words. Words can have multiple meaning, and I am adding a new meaning. This is due

to the First Law of Aristotle’s Logic. Therefore, if gravity cannot be called a force, it is important to get to know about reality.

In other words: according to the Equivalence Principle (Crépin 2019), local physics is independent of space-time curvature. Therefore, gravity is not an interaction. However, in Eq. (2)  $X^{\mu\nu} \neq 0$  is possible; this means that gravity can have much stronger influence than it is currently believed.

But even more beauty is possible if one considers the possibility  $\Lambda = 0$  proposed in Refs. (Kang 2020). Virtual Matter would then be the known energy-momentum tensor, e.g. invisible pressure-free dust or an invisible perfect fluid with a properly chosen sign ( $\pm X^{\mu\nu}$ ).

Hereby the singularity places (and other spacetime problems) could be simply cut out of our Universe map (if necessary), e.g. the event horizon is the edge of our Universe (Martila 2020). This can be the actual reason behind the “information loss paradox”: the vanishing of matter, because a vanishing of matter is already shown (the “abrupt end geodesics” above).

### 6.6 Fixing to Black Hole Information Paradox

The black hole information paradox is a puzzle resulting from the combination of quantum mechanics and general relativity. Calculations suggest that physical information could permanently disappear in a black hole, allowing many physical states to devolve into the same state. This is controversial because it violates a core precept of modern physics. There are two main principles related to it (Hossenfelder 2019): “quantum determinism” means that given a present wave function, its future changes are uniquely determined by the evolution operator; “reversibility” refers to the fact that the evolution operator has an inverse, meaning that the past wave functions are similarly unique. The combination of the two means that information must always be preserved.

Such a description of the information loss paradox implies that the laws of nature are not time-reversible, i.e. are not T-invariant. But that problem can be shown without employing the complicated and imperfect calculations of Hawking, just by understanding that during the gravitational collapse of a dust cloud in co-moving coordinates the process becomes irreversible after the size of the cloud becomes smaller than Schwarzschild radius. This is because “nothing can escape the Black Hole”.

As of November 2019, the paradox may have been resolved, at least for simplified models of gravity (Penington 2019).

## 7 Appendix: abrupt end geodesics

The velocity components of a radial straightline falling of a neutral test-particle in Reissner–Nordström spacetime are given by

$$u^r \equiv \frac{dr}{d\tau} = -\frac{1}{r^2} \sqrt{B}, \quad u^\theta = u^\phi = 0, \quad (4)$$

where  $B = E^2 r^4 - (r^2 - 2Mr + Q^2)r^2$ .

In “geometrized” units ( $Q, M, r$  in meters) let us choose  $Q = 1/5$  and  $M = 1/2$ . Zero initial velocity ( $B = 0$  at  $r = r_0 = 20$ ) determines the trajectory with

$$E = \frac{\sqrt{9501}}{100}. \quad (5)$$

Therefore

$$B = -\frac{499}{10000} r^4 + r^3 - \frac{1}{25} r^2, \quad (6)$$

which is negative in  $r < r_m = 20/499$ . Thus, at  $r_m$  one has  $u^r = 0$ .

This can mean a termination of the falling body. The terminations are present in a Kerr spacetime as well as in naked singularity regimes, and the “smooth correction” of metric (using my Virtual Matter like in Eq. (3)) can remove the singularity. Such terminations were never found yet. Indeed, it is not reported in Refs. (Lightman 1975; Hackmann 2013).

The value of  $E$  in Eq. (5) is slightly different for either slightly different parameter of spacetime ( $a, Q$  or  $M$ ) or for slightly different initial velocities of the test particle. Therefore, my effect holds not for very specific parameters, but has a wide range of physically allowed parameters.

An anonymous referee of some top-ranked journal has written: “The author appears to be concerned about points where  $u^r = 0$ . However, even in the Schwarzschild solution this can happen and it is perfectly harmless. The geodesic equations in the Schwarzschild spacetime, when applied to light deflection, contain a point where  $u^r = 0$ , this is the point of closest approach and it makes perfect sense for this function to go through a minimum which is why its derivative is allowed to vanish. It is “turning point”. This has nothing to do with the termination of a falling body.”

Dear reader, you should not be satisfied by this bizarre report of the referee, as I am talking about a radial straightline falling into the Black Hole, while the referee talks about a curved “passing-by” orbit.

In case of Reissner–Nordström spacetime the direct radial falling is studied, so it has no turning point as imagined by the referee. Moreover, the Kerr spacetime

is considered (Martila 2019), and falling goes along the axis of rotation  $\theta = 0$ . Therefore, it does not have a turning point as well. In case of general falling with  $\theta \neq 0$ , the spacetime point with  $r_m$  has zero velocity for the falling body,  $u^r = u^\theta = u^\phi = 0$ , which points not to a turning point but to a complete stop. This is not the entrance into another universe (in contrast to Ref. (Poisson 2004)), because the stationary observer at this point reports zero kinetic energy, and the latter is not a feature of wormhole spacetimes (Morris 1988). Secondly, at the abrupt end  $r_m$  a “tunnel” or wormhole entrance cannot be found, as the position  $r_m$  depends on the initial velocity of the test particle. Thirdly, the tunnel would have to have its own metric elements, an instance for which there is no sign of existence in the Reissner–Nordström metric; and the tunnel needs exotic matter (Morris 1988), which is absent in the inner vacuum solution of the Reissner–Nordström metric. Because there is only one point with  $u^r = 0$  below the event horizon and no “escape” tunnels, the consequence is the vanishing of the test-particle (because nothing can escape the Black Hole). Finally, considering a falling drop of perfect fluid I have found out (Martila 2019) that the size of the drop vanishes at  $r_m$ .

For this consideration I use a Black Hole with nothing beyond the event horizon, only empty spacetime. It is perfectly known that inside any Black Hole the matter is placed only at the singularity  $r = 0$ . Indeed, many authors, including the authors of Ref. (Hackmann 2013), do study the inner vacuum solution of the Black Hole.

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