

# How to obtain a mass of a graviton, Starting with a first integral and then comparing it with an equivalence between Planck length and a De Broglie wavelength. To obtain early universe entropy. How we can tie this discussion into the influence of the 5<sup>th</sup> dimension in Pre Planckian space-time ? As well as the formation of voids ?

ANDREW WALCOTT BECKWITH

Physics Department, Chongqing University, College of Physics, Chongqing University Huxi Campus, No. 44 Daxuechen Nanlu, Shapinba District, Chongqing 401331, People's Republic of China

[Rwill9955b@gmail.com](mailto:Rwill9955b@gmail.com); [abeckwith@uh.edu](mailto:abeckwith@uh.edu)

## Abstract

Using the Klauder enhanced quantization as a way to specify the cosmological constant as a baseline for the mass of a graviton, we eventually come up and then we will go to the relationship of a Planck Length to a De Broglie length in order to link how we construct a massive graviton mass, with cosmological constant and to interface that with entropy in the early universe. We then close with a reference to the possible quantum origins of e folding and inflation. This objective once achieved is connected with a possible mechanism for the creation of voids, in the later universe, using a construction of shock fronts from J. P Onstriker, 1991 and followed up afterwards with Mukhanov's physical foundations to Cosmology book section as to indicate how variable input into self reproduction of the Universe structures may lead to void formation in the present era. A connection with Wesson's 5 dimensional cosmology is brought up in terms of a generalized uncertainty principle which may lead to variations of varying energy input into self reproducing cosmological structures which could enable non uniform structure formation and hence voids. One of the stunning results is that the figure of number of gravitons, about  $10^{58}$ , early on, is commensurate with a need for negative pressure, (middle of manuscript) which is a stunning result, partly based on Volovik and weakly interacting Bose gas model for pressure, which is completely unexpected.

## 1. Start with the General Relativity First integral.

We use the Padmanabhan 1<sup>st</sup> integral [1], of the form , with the third entry of Eq. (1) having a Ricci scalar defined via [9] and usually the curvature  $\mathfrak{R}$  set as extremely small, with the general relativity[2], [3]

$$\begin{aligned} S_1 &= \frac{1}{2\kappa} \int \sqrt{-g} \cdot d^4x \cdot (\mathfrak{R} - 2\Lambda) \\ \& - g &= -\det g_{uv} \\ \& \mathfrak{R} &= 6 \cdot \left( \frac{\ddot{a}}{a} + \left( \frac{\dot{a}}{a} \right)^2 + \frac{\mathfrak{K}}{a^2} \right) \end{aligned} \quad (1)$$

Also, the variation of  $\delta g_{tt} \approx a_{\min}^2 \cdot \phi$  as given by [4,5] will have an inflaton,  $\phi$  given by[6]. Leading to the inflaton which is combined into other procedures for a solution to the cosmological constant problem. Here,  $a_{\min}$  is a minimum value of the scale factor and is not zero, but close to it.

### 1a. Next for the idea from Klauder

We are going to go to page 78 by Klauder [3] of what he calls on page 78 a restricted Quantum action principle which he writes as:  $S_2$  where we write a 1-1 equivalence as in [1], which is also seen in [2]

$$S_2 = \int_0^T dt \cdot [p(t)\dot{q}(t) - H_N(p(t), q(t))] \approx S_1 = \frac{1}{2\kappa} \int \sqrt{-g} \cdot d^4x \cdot (\mathfrak{R} - 2\Lambda) \quad (2)$$

Our assumption is that  $\Lambda$  is a constant, hence we assume then the following approximation, from[2] which is the precursor of activity as given in [3,4,5, 6] we have

$$\begin{aligned}
\frac{p_0^2}{2} &= \frac{p_0^2(N)}{2} + N; \text{ for } 0 < N \leq \infty, \text{ and } q = q_0 \pm p_0 t \\
V_N(x) &= 0; \text{ for } 0 < x < 1 \\
V_N(x) &= N; \text{ otherwise} \\
H_N(p(t), q(t)) &= \frac{p_0^2}{2} + \frac{(\hbar \cdot \pi)^2}{2} + N; \text{ for } 0 < N \leq \infty
\end{aligned} \tag{3}$$

Our innovation is to then equate  $q = q_0 \pm p_0 t \sim \phi$  and to assume small time step values. Then as in [6]

$$\Lambda \approx \frac{-\left[ \frac{V_0}{3\gamma-1} + 2N + \frac{\gamma \cdot (3\gamma-1)}{8\pi G \cdot \tilde{t}^2} \right] + \left( 6 \cdot \left( \frac{\ddot{a}}{a} + \left( \frac{\dot{a}}{a} \right)^2 \right) \right)}{\frac{1}{\kappa} \int \sqrt{-g} \cdot d^3x} \Bigg|_{t=\tilde{t}} \tag{4}$$

These are terms within the bubble of space-time given in [1] using the same inflaton potential. The scale factor is presumed here to obey the value of the scale factor in [7]

## 2. Why this is linked to gravity/massive gravitons, and possibly early universe entropy

Klauder's program[3] is to embed via Eq.(3) as a quantum mechanical well for a Pre Planckian-system for inflaton physics as given by Eq. (3). as given in Klauder's treatment of the action integral as of page 87 of [3] where Klauder talks of the weak correspondence principle, where an enhanced classical Hamiltonian, is given 1-1 correspondence with quantum effects, in a non-vanishing fashion. If so, by Novello [8] and Eq. (3) we have then for early universe conditions, that we will be leading up to using an algorithm for massive gravitons, as in [6], and [8]

$$m_g^2 = \left( \frac{\hbar \cdot \sqrt{\Lambda}}{c} \right)^2 \approx \frac{\hbar^2}{c^2} \left[ \frac{-\left[ \frac{V_0}{3\gamma-1} + 2N + \frac{\gamma \cdot (3\gamma-1)}{8\pi G \cdot \tilde{t}^2} \right] + \left( 6 \cdot \left( \frac{\ddot{a}}{a} + \left( \frac{\dot{a}}{a} \right)^2 \right) \right)}{\frac{1}{\kappa} \int \sqrt{-g} \cdot d^3x} \right]_{\tilde{t}=t(\text{Planck})} \tag{5}$$

The long and short of it is, to tie this value of the cosmological constant, and the production of gravitons due to early universe conditions, to a relationship between De Broglie wavelength, Planck length, and if the velocity  $v$  gets to a partial value close to the speed of light, that, we have, say by using [11] as given by Diosi, in Dice (2018) for quantum systems, if we have instead of a velocity much smaller than the speed of light, a situation where the particle moves very quickly ( a fraction of the speed of light) that instead of the slow massive particle postulated in [11]

$$\begin{aligned}
\lambda_{\text{De-Broglie}} &\approx \frac{2\pi\hbar}{m_g v} \cdot \sqrt{1 - \frac{v^2}{c^2}} \cong \ell_{\text{Planck}} \approx \sqrt{\frac{\hbar G}{c^3}} \\
\Rightarrow \text{if } v(\text{particle}) &\rightarrow c - \xi^+; \text{ then} \\
\varepsilon(\text{energy - particle}) &\approx E_{\text{Planck}} (\text{Planck - energy})
\end{aligned} \tag{6}$$

If so then, we will be looking at using Ng version of entropy via use of infinite quantum Statistics, [12] we have for a clearly specified value of mass of the graviton, say  $m_g \approx 10^{-62}$  grams as in [13], then we have for the negative components

We are specifying here,

$$\begin{aligned}
\text{If } c \equiv 1, m_g &\approx 10^{-62} \text{ grams,} \\
E_{\text{Planck}} (\text{Planck - energy}) &\equiv 2.18 \times 10^{-5} \text{ grams} \quad (7) \\
&\equiv (m_g \approx 10^{-62} \text{ grams}) \times N(\text{entropy - number}) \\
&\Rightarrow N(\text{entropy - number}) \equiv 10^{58} \equiv 10^{\mathbb{N}}, \text{ and } \therefore \mathbb{N} \equiv 58
\end{aligned}$$

### 3. Can this tie in with early universe e folds ? i.e. from [14] e folds are between 55 to 60

E folds in cosmology are a way of delineating if we have enough expansion of the universe is in line with inflation. As seen in [11] we can have

$$\mathbb{N}(e - \text{fold}, \text{cos mol}) \approx -\int dt \cdot H(\text{cos mol}) \quad (8)$$

Where  $H(\text{cos mol})$  is a value of the Friedman equation, and if we use [13] be defined via that the potential energy,  $V$ , of initial inflation is initially over shadowed by the contributions of the Friedman equation,  $H$ , at the onset of inflation. Then

$$\mathbb{N}(e - \text{fold}, \text{cos mol}) \approx 55 - 60 \quad (9)$$

What we wish to explore will be if Eq. (9) above is consistent with

$$N(\text{entropy - number}) \equiv 10^{58} \equiv 10^{\mathbb{N}}, \text{ and } \therefore \mathbb{N} \equiv 58 \quad (10)$$

Doing so may involve use of the Corda article, as given in [12]

### 4. Now for foundational treatment as to if we may have an influence of the 5<sup>th</sup> dimension in our problem.

Wesson, [13] has a procedure as far as a five dimensional uncertainty principle which is written as, if  $n = L/l$

Where  $L$  is for 4<sup>th</sup> dimensions, and  $l$  is a five dimensional representation where  $l = h/mc$  and we have

$$dS_5^2 = \left(\frac{L}{l}\right)^2 ds_4^2 - \left(\frac{L}{l}\right)^4 dl^2 \quad (11)$$

Such that

$$\begin{aligned}
|dp_\alpha dx^\alpha| &= \frac{h}{c} \cdot \frac{dn^2}{n} \\
&\xrightarrow{\alpha \rightarrow 0, \text{Pre-Planckian}} \\
|dp_0 dx^0| &= \frac{h}{c} \cdot \frac{dn^2}{n} = \left| \frac{dE}{c} \cdot c dt \right| \quad (12) \\
&\Rightarrow |dE \cdot dt| \approx \int \frac{h}{c} \cdot \frac{dn^2}{n} \\
&\xrightarrow{h=c=1, \text{Pre-Planckian}, n=L/l} \\
|\Delta E \cdot \Delta t| &\approx n \cdot (\ln n - 1)
\end{aligned}$$

Using a n expansion of the form from CRC tables[14]

$$\ln_e n = (n-1) - \frac{1}{2} \cdot (n-1)^2 + \frac{1}{3} \cdot (n-1)^3 + \dots \quad (13)$$

Up to cubic roots we obtain one real root and 2 conjugate complex roots of, if we use minimum uncertainty of  $\Delta E \Delta t = \hbar \rightarrow 1$ , and set c=1, we have then

$$\begin{aligned} n_1 &\approx 1.54715 \\ n_2 &\approx .42643 + 1.2242i \\ n_3 &\approx .42643 - 1.2242i \end{aligned} \quad (14)$$

If so for the real case, of n, we have about the Planckian regime we look at

$$l = \frac{l(\text{Planck}) = l_p}{1.54715} \quad (15)$$

We will then look at the consequences of the real root, first, in terms of variation of minimum time step before going to other cases, but for the record, we have then the weird case of , for real root n in eq. (14) that

$$\Delta t \approx \frac{-.845184}{\Delta E} \quad \text{real iff } \Delta E < 0 \quad (16)$$

##### 5. Under what conditions would $\Delta E < 0$ ? How would negative energy tie into negative Pressure which is normally expected in the onset of inflation?

First of all, look at conditions for rapid acceleration of the Universe, i.e. to have this according to the GR theory we have by [15] if a(t) is a scale factor, then the Friedman equations read as

$$\begin{aligned} \frac{\ddot{a}}{a} &= -\frac{4\pi G_N}{3} \sum_j (\rho_j + 3p_j) + \frac{\Lambda_b}{3} \\ \text{If } a(t) &= a_{\min} t^\alpha \quad \text{then if } j=1(\text{gravitons}) \\ 3\alpha^2 - 3\alpha + 4\pi G_N (\rho + 3p) &= \Lambda_b \end{aligned} \quad (17)$$

Now, look at a concept of pressure. Here. If the first expression is tabulated about Planck time (or just before)

$$\begin{aligned} \Lambda &\approx \frac{-[p(\tilde{t})\dot{q}(\tilde{t}) - H_N(p(\tilde{t}), q(\tilde{t}))]}{\frac{1}{\kappa} \int \sqrt{-g} \cdot d^3x} \\ &+ \frac{\frac{1}{2\kappa} \int \sqrt{-g} \cdot d^3x \cdot \left( \Re = 6 \cdot \left( \frac{\ddot{a}}{a} + \left( \frac{\dot{a}}{a} \right)^2 + \frac{\aleph}{a^2} \right) \right) \Big|_{t=\tilde{t}}}{\frac{1}{2\kappa} \int \sqrt{-g} \cdot d^3x} = 3\alpha^2 - 3\alpha + 4\pi G_N (\rho + 3p) = \Lambda_b \end{aligned} \quad (18)$$

We can then make the identification that we have negative pressure, we then have if we have both pressure and energy negative then we can make the following pairing of terms, i.e. first for the negative terms in Eq.(18)

$$\begin{aligned}
& \text{If } a(t) = a_{\min} t^\alpha \text{ then if } j=1(\text{gravitons}) \\
& 3\alpha^2 - 3\alpha + 4\pi G_N (\rho + 3p) = \Lambda_b \\
& \text{and } \Lambda_b = \Lambda \text{ from Eq.(4)} \\
& \Rightarrow -\frac{6p_{\text{momentum}}(t)\dot{q}(t) \cdot \kappa}{2 \cdot \int \sqrt{-g} d^3x} = -3\alpha - 12\pi G_N \cdot |P_{\text{pressure}}|
\end{aligned} \tag{19}$$

Momentum and the time derivative of “space” are in the last line of Eq(19) specified as of the interior up to the boundary of a space-time bubble defined by  $a_{\min}$  for the left hand side of Eq(19) , last line.

We will after this is described go to the positive terms in Eq.(18). We get then

$$\begin{aligned}
& \text{If } a(t) = a_{\min} t^\alpha \text{ then if } j=1(\text{gravitons}) \\
& 3\alpha^2 - 3\alpha + 4\pi G_N (\rho + 3p) = \Lambda_b \\
& \text{and } \Lambda_b = \Lambda \text{ from Eq.(4)} \\
& \Rightarrow \left. \frac{|H_{\text{Potential-well-Hamiltonian}}(p_{\text{momentum}}(t)q(t)) \cdot \kappa}{2 \cdot \int \sqrt{-g} d^3x} + 6\left(\alpha^2 + \frac{\aleph}{a_{\min}^2 t^{2\alpha}}\right) \right|_{t=t(\text{Planck})} \\
& = 6\alpha + 4\pi G_N |\rho_{\text{early-universe-density}}|
\end{aligned} \tag{20}$$

We will then be looking at how we can then equate out a negative energy and a negative pressure for this Pre Planckian to Planckian physics transition.

## 6. Explicit calculation for a negative pressure in this Pre Planckian to Planckian physics transition

We will transition to Reference [15] by Volovik, 2003 which has the following expression for pressure in a vacuum state of weakly interacting Bose Gases. i.e.

$$\begin{aligned}
P_{\text{Bose-fluid}} &= \frac{1}{2\hbar^3} \sqrt{-g} \cdot \left( E_{\text{Planck}2}^3 E_{\text{Planck}1}^1 - \frac{16}{15\pi^2} E_{\text{Planck}1}^4 \right) \\
&\& E_{\text{Planck}1}^1 = mc^2, \\
E_{\text{Planck}2}^1 &= \hbar c / \Theta, \\
\Theta &\sim \sqrt[3]{n(\text{particle-density})} \sim n^{1/3}
\end{aligned} \tag{21}$$

For our problem if we configure the initial contents of the “well” we assume for having a near singularity, for space-time expansion start we can have  $n = N/V$  , with  $N$  as the number of would be “gravitons, , and  $V$  being the “Volume of space-time for our evaluation”. Whereas,  $m = N$  times the mass of a graviton. If so a simple calculation for this problem would have, then a negative value for pressure if we have the following, namely

$$E_{Planck2}^3 < \left( \frac{16}{15\pi^2} \right) \times E_{Planck1}^3 \quad (22)$$

$$\Rightarrow \hbar c / \left( N_{gravitons} m_{graviton} / Vol \right)^{1/3} < \left( \frac{16}{15\pi^2} \right)^{1/3} \times N_{gravitons} m_{graviton} c^2$$

Here, use  $m_{graviton} \leq 10^{-62} - 10^{-65}$  grams which is from [16], and Planck Mass  $m_{Planck} \approx 2.176 \times 10^{-5}$  grams [17]

Use, here that Vol = (Planck length, cubed) times 1/(1.54715), cubed = Planck length, cubed times 0.27002422918

Therefore if we use Planck length set equal to 1 and h bar = 1 and Planck mass = 1, we have Eq. (22) re written as

$$\left( \frac{15\pi^2}{16} \right)^{1/3} \times .27002422918 \leq (.5 \times 10^{-58} m_{Planck})^{4/3} N_{graviton}^{4/3} \quad (23)$$

Or roughly

$$\left( \frac{15\pi^2}{16} \right)^{1/3} \times .27002422918 \leq 10^{-77} N_{graviton}^{4/3} \Rightarrow 10^{77} \leq N_{graviton}^{4/3} \quad (24)$$

Or an upper bound of say for graviton mass of  $10^{-62}$  grams, we have that we have negative pressure in our system for the number of gravitons being less than  $10^{58}$ , in a volume about .27 times the cube of Planck length. This is stunning because in Eq.(7) we have an entropy number of  $10^{57}$  to  $10^{58}$ , which is amazing because it suggests that the entropy generation we pick is tied in explicitly for the generation of negative pressure which is essential for inflation.

7. **Now for how we could consider having  $\Delta E$  drop as negative energy, in our problem of Pre-Planckian physics right before the onset of inflation. With a flip over to ultra high temperature- energy conditions.**

From [18] we have the following relationship, i.e. see referenced [18] have in its Eq.(8) the following value

$$E = \frac{d}{2} PV$$

$$d = \text{dim}, \quad (25)$$

$$P = \text{Pressure}$$

$$V = \text{Volume}$$

The discussion as to implementation of Eq. (25) has that if the conditions in section 6 above are obtained for negative pressure, that in the Pre Planckian state we have at a chance, a quadratic dispersion relationship. In addition, Reference [18] claims that this is a result of a derivation from the Virial theorem as given in [19], so then that we may look at

$$\begin{aligned}
& \text{(Heisenberg)} \frac{dP}{dt} = \frac{i}{h} [H, P] \xrightarrow{[P, X] = \frac{\hbar}{i}} \frac{dP}{dt} = -V'(X) \\
& \Leftrightarrow \text{(Schrodinger - Ehrenfest Theorem)} \frac{d\langle P \rangle}{dt} = -\langle V'(X) \rangle \\
& \& \text{(Schrodinger)} \frac{d\langle P \rangle}{dt} = -\langle V'(X) \rangle \text{ for classical } \frac{dP}{dt} = -V'(X) \\
& \Leftrightarrow \text{(Heisenberg)} \frac{dP}{dt} = \frac{i}{h} [H, P] \xrightarrow{[P, X] = \frac{\hbar}{i}} \frac{dP}{dt} = -V'(X)
\end{aligned} \tag{26}$$

This is in a way of referring to [18] and [19] a way to ascertain the correctness of using Eq. (25) in the Pre-Planckian to Planckian transition in space-time

Having said that. We will then state that what we believe is that V as volume, as given in Eq. (25) would be roughly about .27 times the cube of Planck length, as a starting point, for investigation and that we would then have a transition up to the Planck length. Prior to nucleation of space-time

Our hypothesis, is that breaching the barrier to full emergence would entail a simultaneous flip from negative (bound energy states) to Positive energy, whereas we would be using a variant of positive energy given as'

$$E(\text{inf}) \sim \frac{d}{2} \cdot k_B \cdot T_{\text{inf}} \tag{27}$$

i.e. a release of bound state to unrestrained positive energy would be commenced from the Pre Planckian to Planckian transition.

i.e. eventually, if there is a barrier, of space-time at the surface of a sphere of about .27 times the cube of Planck length, in "volume" that when the barrier was breached, there would be a switch from negative energy, to positive energy, but that the pressure would still be negative, hence "inside" the initial near singularity sphere we would have a negative value of Eq.(27) signifying a BOUND state. Once the barrier collapsed, Eq. (27) would switch to positive, but that in lieu of inflation that the pressure of our system would still follow Eq. (21) and Eq. (22)

**All this may be tied into an issue of semi classical reasoning as given below. We include this in to motivate readers to consider how a semi classical set of approximations may lead to bridging the gap between General Relativity and Quantum mechanics. We argue that the challenge in our present problem is to re duplicate the same methodology, but to also find a suitable potential system, instead of just a hierarchy of kinetic energy expressions.**

**8. Lesson learned, i.e. a way to ascertain if quantum gravity has a chance to be applied Quantum Geometrodynamics and Semi classical approximations, as reference [20] and evolutionary Equations, for quantum states, and its relationships to quantum issues arising in [21]**

We wish now to refer to another result which we view as largely in tandem with our quest as to come up with precursors to quantum gravity, i.e. from Kieffer.

Due to how huge this literature is, we will be by necessity restricting ourselves to pages 172 to 177 of [20] as that encompasses Hamiltonian style formalism and also has some connections to the Hamilton Jacobi equation.

We will make this limitation so our methods are not too far removed from the Solvay conference, 1927, i.e. the Hamilton-Jacobi equation makes an appearance, as well as a full stationary Schrodinger equation.

In this discussion, the wave functions are often quantized, or nearly so, albeit usually added gravitational background is semi classical.

To begin our inquiry as to Geometrodynamics, which has some fidelity to the Solvay 1927 conference, we look at the following expansion of the Klein Gordon Equation, without an external potential. i.e.

$$\begin{aligned}
& \left( \frac{\hbar^2}{c^2} \cdot \frac{\partial^2}{\partial t^2} - \hbar^2 \Delta + m^2 c^2 \right) \Psi_{KG} = 0 \\
& \& \\
& \Psi_{KG} = \exp(i \cdot S_{example} / \hbar) = c^2 S_0 + S_1 + c^{-2} S_2 + \\
& \& \\
& S_0 \sim \pm m \cdot t \Rightarrow \left( \Psi_{KG} \text{ at } c^2 \right) \sim \exp(-imc^2 t / \hbar) \\
& \& \\
& \left( \Psi_{KG} \text{ at } c^0 \right) \sim \exp(iS_1 / \hbar) \Rightarrow i\hbar \Psi_t = \frac{-\hbar^2}{2m} \Delta \Psi \\
& \& \\
& \left( \Psi_{KG} \text{ at } c^{-2} \right) \sim \exp(iS_2 / \hbar) \Rightarrow i\hbar \Psi_t = \frac{-\hbar^2}{2m} \Delta \Psi - \frac{\hbar^4}{8m^3 c^2} \Delta \Delta \Psi \\
& \& \\
& \frac{\hbar^4}{8m^3 c^2} \Delta \Delta \Psi = \text{first - relativistic - correction - term} \tag{28}
\end{aligned}$$

As a Klein Gordon result, this leads directly to the idea of quantum mechanics, as embedded within a larger theory.

I,e this methodology as brought up by Kieffer, in page 177 of [20] in its own way is fully in sync with some of the investigations of the embedding of quantum mechanics within a larger structure, as has been mentioned in a far more abstract manner by t'Hooft, in [22], although to make further connections, it would be advisable to have a potential term put in, as well as to have more said about relativistic corrections.

As mentioned by [22] , Lammerzahl , C. in [23] has extended this sort of reasoning to quantum optics in a gravitational field. The virtue of this, is that one is NOT using the functional Schrodinger equation, as seen in page 149 of the Wheeler De Witt equations, given in [20]. i.e. the above derivation, within the context of the orders of c, given above, has explicit time dependence put in its evolution equations, and avoids some of the issues of the Wheeler De Witt program. I.e. read page 149 and beyond in [20] as to some of the perils and promises as to this approach.

In addition the  $c^0$  recovery of the Schrodinger equation, and the  $c^{-2}$  recovery of a Schrodinger equation within the context of the Klein Gordon equation is fully in sync with some of the Solvay 1927 deliberations. As given in [21]. And also directly linkable to [22]



What we wish to do is to re duplicate the same sort of power expansion picking off of terms given in Eq. (28) but instead of using the Klein Gordon Equation, without a potential, to use a similar equation with a potential and from there to ascertain an embedding of space time effects largely in sync with t'Hooft as given in [22] at near the Plank regime of space time. Doing so would among other things employ a re do and looking at how our evolution equation so chosen, as mentioned in Eq. (28) may be linked to the issues given in Eq. (3) and Eq. (4) of our manuscript

However, before tying an evolution Equation, from Eq. (28) suitably modified to use parts of Eq. (3) and Eq. (4) we need to consider if we have a Hamiltonian system which is the same as the ENERGY of a system. If we do not have this option, it is a good bet that the system so modeled does NOT conserve energy. Ie. What would that mean for our problem?

**9. A major caution to consider, i.e. when we have a Hamiltonian which is not conserved, i.e. when Hamiltonian H no longer is in sync with the ENERGY E of a system**

Very simply put, if the Hamiltonian has for any reason a time component to it, so the time derivative of a Hamiltonian is not zero, then the physically modeled system is not conserving energy. i.e. for a Lagrangian L, we have that by [24]

$$\varepsilon(\text{energy}) = \dot{q}_\beta \frac{\partial L}{\partial \dot{q}_\beta} - L \quad (29)$$

Whereas we can write if L has no time dependence , that

$$\frac{d\varepsilon(\text{energy})}{dt} = -\frac{\partial L}{\partial t} = 0, \text{ if } L \neq L(t) \quad (30)$$

The Lagrangian L = Kinetic energy – Potential energy, hence if we go to look at the Hamiltonian itself we have

H(Hamitonian)=Kinetic energy+ Potential energy) = Total energy E, iff

$$\frac{dH}{dt} = 0 \Leftrightarrow H = \varepsilon(\text{energy}) \quad (31)$$

Otherwise, we have

$$\frac{dH}{dt} \neq 0 \Leftrightarrow H \neq \varepsilon(\text{energy}) \quad (32)$$

What we have to decide in terms of the evolution of Eq. (3) and Eq.(4) is do we have a closed or an open physical input into the creation of the Universe. This will profoundly influence how we look at Eq. (20) above, which in turn has a lot to say about how uniformly applicable Eq. (24) actually is. i.e. if we do this, then there is a matter of the self reproduction of the Universe as given by Mukhanov, [25] where we have for a scalar field driving the expansion of the universe, with a scalar field being bigger than the square root of the mass of the universe for domain production as given in [25] , page 353.

## 10. What if we wish to consider Mukhanov Self reproduction of the Universe criteria?

First of all we will give pertinent background before we go to the Mukhanov criteria.

Note that from [1,26] we have

$$a(t) = a_{\min} \cdot t^\gamma \quad (33)$$

Leading to [1] the inflaton.

$$\phi \approx \sqrt{\frac{\gamma}{4\pi G}} \cdot \ln \left\{ \sqrt{\frac{8\pi G V_0}{\gamma \cdot (3\gamma - 1)}} \cdot t \right\} \quad (34)$$

And then we can look at the consequences for self reproduction of the universe, given on page 353 of [25] and its figure 8.7 as seen in page 353, of [25] with a perpetuating continual expansion of the universe, given a mass,  $m$ , for which the scalar field of Eq. (34) obeys

$$\phi > m^{1/2} \quad (35)$$

If we use Clifford Will, as in [16] for velocity of a massive graviton and make the following substitutions, we will have

$$\begin{aligned} \gamma &\rightarrow \alpha \\ \Delta E &= N_g m_g \cdot c^2 \cdot \left( 1 - \frac{m_g^2}{E^2 = \hbar^2 \cdot \omega_g^2} \right) \\ \Rightarrow \Delta t_{\min} &\approx \frac{\hbar}{N_g m_g \cdot c^2 \cdot \left( 1 - \frac{m_g^2}{E^2 = \hbar^2 \cdot \omega_g^2} \right)} \propto t \end{aligned} \quad (36)$$

Then we have the inequality for self reproduction of the universe as

$$\sqrt{\frac{8\pi G V_0}{\alpha \cdot (3\alpha - 1)}} \frac{\hbar}{N_g m_g \cdot c^2 \cdot \left( 1 - \frac{m_g^2}{\hbar^2 \cdot \omega_g^2} \right)} \geq \exp \left( \sqrt{\frac{4\pi G}{\alpha}} \cdot \sqrt{N_g m_g} \right) \quad (37)$$

Also keep in mind the numerical density  $N$ , as given above, can be linked to a "particle count" due to Entropy

Then using Kolb and Turner[27], we would see say,

$$s(\text{entropy} - \text{density}) = \frac{2\pi^2}{45} g_* \cdot \left( T_{\text{universe}} / T_{\text{Planck}} \right)^2 \quad (38)$$

And if we have utilization of  $N(\text{particle count}) \sim S(\text{entropy})$  as given in [28] by  $N_g$ , if we solve conclusively for

$N_g$  from utilizing Eq. (37) we have that, we can re write Eq. (38) to read as implying

$$\begin{aligned} \left[ N_g / Vol(in - Planck - units) \right] &\sim s(entropy - density) = \frac{2\pi^2}{45} g_* \cdot \left( T_{universe} / T_{Planck} \right)^2 \\ \Rightarrow \left( T_{universe} / T_{Planck} \right)^2 &\approx \left( \frac{2\pi^2}{45} g_* \right)^{-1} \cdot \left[ N_g / Vol(in - Planck - units) \right] \end{aligned} \quad (39)$$

Should the value of  $N_g \propto 10^{58}$  as by earlier arguments in this manuscript, as stated, then if the value of

$g_* \sim N_g \propto 10^{58}$  in the case that we have  $\left( T_{universe} / T_{Planck} \right)^2 \approx 1$ , or so, in the early Pre Plankian to Planckian transition, i.e. it means that just prior to the transition to the inflationary regime that we have the following situation

As given on page44 of [29]

$$\begin{aligned} v_{shock-wave} &\approx \sqrt{E / m} \\ R_{shock-wave} &\approx v_{shock-wave} t \\ m &\approx \rho R_{shock-wave}^3 \\ \Rightarrow R_{shock-wave} &\approx \left( E \cdot t^2 / \rho \right)^{1/5} \end{aligned} \quad (40)$$

This shock wave has to be compared with  $\Delta t \approx \frac{-.845184}{\Delta E}$  *real iff*  $\Delta E < 0$ , whereas we were discussing a situation for the diminuation of energy at the start of expansion. As for what I am referring to, see , if we reference variation of change of temperature  $\Delta T_{universe}$  against scale factor  $a(t)$  as given in page 401 of [30] with  $\Delta T_{universe}$  decreasing in value as to expanding scale factor size  $a(t)$ , hence Eq. (41) below would be negative.

$$\Delta E \approx \frac{d(dim)}{2} \cdot k_B \cdot \Delta T_{universe} \quad (41)$$

In doing so, we would then in this case see if we use the real root of n, given in Eq. (14) above

$$\Delta t \approx \frac{2 \times .845154}{d(dim) \cdot k_B \cdot |\Delta T_{universe}|} \quad (42)$$

Then a shock front, right at the starting gate of expansion would look like for the first root of n, in Eq. (14)

$$\begin{aligned} R_{shock-wave} &\approx \left( E \cdot t^2 / \rho \right)^{1/5} \\ &\approx \left( 2 \times (.845154)^2 / d(dim) \cdot k_B \cdot |\Delta T_{universe}| \right)^{1/5} \times \left( 1 / N_g \cdot m_g \cdot (V_{Volume}) \right)^{1/5} \end{aligned} \quad (43)$$

Here the volume, in this case would be .27 times the cube of Planck length, and the mass of a graviton is approximately  $10^{-62}$  grams

## 11. Conclusion, i.e. self reproduction of the universe may entail varying values of Eq. (43) if we look at three roots of n given in Eq. (14), which influences a minimum time step

We state that using the conjugate complex roots of n given in Eq. (14) would lead to different values of the numerator of Eq. (43) which would lead to different values of Eq. (43). We argue that this would induce chaos, and voids in subsequent evolution of space-time. i.e. a matter which we intend to numerically investigate if we have 3 different complementary n values in play used as to Eq. (14) and Eq.(43)

Keep in mind that if we use the values of  $m_{Planck} \approx 10^{58} \times m_{graviton} = \hbar = k_B = 1$  due to renormalization, then Eq. (43) becomes if we also assume Planck length scaled to 1 so then we have

$$\begin{aligned} R_{shock-wave} &\approx \left( E \cdot t^2 / \rho \right)^{1/5} \\ &\approx \left( 2 \times (.845154)^2 / d(\dim) \cdot k_B \cdot |\Delta T_{universe}| \right)^{1/5} \times \left( 1 / N_g \cdot m_g \cdot (V_{Volume}) \right)^{1/5} \quad (44) \\ &\approx \left( 2 \times (.845154)^2 / d(\dim) \cdot |\Delta T_{universe}| \right)^{1/5} \times (1 / .27)^{1/5} \end{aligned}$$

This is obviously semi classical, and we will ask readers to consider that what may be used to add more rigor to our analysis would be the process of Bosonification, as seen in [31], page 319-369 of R. Shankar , with the caveat that we would be considering perhaps using advanced field theory , to have relativistic Dirac Fermions obeying Standard Anti Commutation rules by a Boson field theory. The Fermions would be super partners to the spin two gravitons which in SUSY are spin 3/2 gravitinos.

If SUSY is a non starter, and there have been no confirmed data sets for SUSY out of CERN, then we may have to be using gravitons and lump it.

Eq. (44) is for the real root of Eq. (14). Very likely the two complex roots of Eq. (14) would yield different numerator values for the shock wave front formula, and the mixing of all three versions of shock waves, would be itself enough to induce chaos, or at least some of the phenomenology seen in [32]. And if we are lucky in our formulation we may be able to get a potential added to the deliberations of Eq. (28), in terms of hierarchy of embedding space time in terms of a power law development. To do that though would require identifying though a suitable potential added, and we need to find that commensurate potential.

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