

# Why an Albedo Solution to Global Warming is 2.6 Times Better

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## Abstract

In this paper, modeling finds a 2.6 times advantage in an albedo global warming solution compared to a greenhouse gas (GHGs) resolution. A key difference in our assessment is the inclusion of a fractional re-radiation from GHGs as part of the shortwave length albedo absorption assessment that occurs. Using this view, along with an interesting albedo-Planck parameter, it is concluded that a 1.5% solar geoengineering change in the global albedo could result in a significant solution in global warming mitigation and would be vital in preventing a tipping point from occurring.

## 1 Introduction

In our race against time in global warming, it may be appropriate to ask the question, what are the best solutions rather than addressing what is viewed as the main problem. To address this question, we create a model that uses a re-radiation factor, which helps to quantify significant differences between changes in the global albedo versus greenhouse gas forcing (the two main solutions to global warming). The re-radiation parameter is obtained mainly in equilibrium modeling with appropriate interactions and constraints to aid in comparison; the re-radiation parameter is then found in the absence of warming feedbacks with a unique value of 0.612 (or  $\beta=0.887$ ). The re-radiation factor is a redefined variable taken from the effective emissivity constant of the planetary system. Then, the Planck's feedback parameter is used to verify model consistency. The model illustrates a reasonable way to view the Earth's energy budget; it provides a number of useful insights in climatology sensitivity estimates and demonstrates the relative advantage of solar geoengineering solutions over GHG reduction in global warming mitigation [1]. Specifically, a larger albedo advantage of 2.6 is found. Results also suggest that a 1.6 re-radiation factor could be added to  $\lambda_\alpha$  [2]. In working the model, we also find a handy Planck-Albedo parameter that may be useful to climatologists [3] having a convenient value of  $1\text{W/m}^2/\text{K}/\Delta\%\text{albedo}$  and this is used to help illustrates the benefits in equilibrium assessments. In a companion paper [1] we suggest how to implement the albedo solution.

## 2. Data and Method

To introduce the re-radiation surface model, we will often refer to the Planck parameter and its associated functions that play a key role in development and verifying this model. Therefore, we provide an overview in Appendix A which also includes a unique way to assess its value using an albedo approach (see A.1).

### 2.1 The Re-radiation Global Warming Model

In this model we define

$$P_{Total} = \sigma T_S^4 = \sigma \left( \frac{T_{TOA}}{\beta} \right)^4 \quad \text{and} \quad P_\alpha = \sigma T_\alpha^4 = \sigma (\beta T_S)^4 \quad (1)$$

The definitions of  $T_{TOA}$ ,  $T_S$  and  $\beta$  are provided in Appendix A (Eq. A-1, A-2, A-3). We consider a time when there is *no feedback issues*. Then by conservation of energy, the equivalent power re-radiated from GHGs in this model is dependent on  $P_\alpha$

$$P_{GHG} = P_{Total} - P_\alpha = \sigma T_S^4 - \sigma T_\alpha^4 \quad (2)$$

To be consistent with Eq. A-1,  $T_\alpha = T_{TOA}$ , since typically  $T_\alpha \approx 255^\circ\text{K}$  and  $T_S \approx 288^\circ\text{K}$ , then we note in keeping the definition of Beta (see Eq. A-4) for the moment  $\beta \approx T_\alpha/T_S \approx T_{TOA}/T_S$ .

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This allows us to write the dependence

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$$P_{GHG} = \sigma T_S^4 - \sigma T_\alpha^4 = \frac{\sigma T_\alpha^4}{\beta^4} - \sigma T_\alpha^4 = \sigma T_\alpha^4 \left( \frac{1}{\beta^4} - 1 \right) \quad (3)$$

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We note that when  $\beta^4=1$ , there are no GHGs contributions as required. We now define a re-radiation parameter  $f = \beta^4$ . We know that some fraction of the blackbody radiation is re-radiated by the GHGs, so  $f$  is a re-radiation parameter. That is, the energy,  $P_{GHG}$ , must be some fraction of  $P_\alpha$  so that its dependence is also

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$$P_{GHG} = f P_\alpha = f \sigma T_\alpha^4 \quad (4)$$

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This is a key difference in how we view the total effect from short wavelength absorption with the inclusion of re-radiation [2]. Now in order for this to be true, we require from Equations 3 and 4

72

$$P_{GHG} = \sigma T_\alpha^4 \left( \frac{1}{f} - 1 \right) = f \sigma T_\alpha^4 \quad (5)$$

This dependence leads us to the solution of the quadratic expression

75

$$f^2 + f - 1 = 0 \text{ yielding } f_1 = 0.618034 = \beta^4, \beta = (0.618034)^{1/4} = 0.88664 \quad (6)$$

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This is very close to the value estimated for  $\beta$  and this has been obtained through energy balance in the planetary system providing a completely self-determining assessment without approximations. In Section 2.6, we double check this model in another way by balancing energy in and out and in Section 3 we will apply the modeling to demonstrate its capability.

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## 2.2 Re-radiation Model Applied to Two Different Time Periods

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Global warming can be modeled by looking at two different time periods. We can model the radiation for 1950 as due to blackbody radiation with the addition of GHG re-radiation where in this period

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- we will assume no feedback issues causing a warming trend so that from our model

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$$P_{Total\_1950} = P_\alpha + P_{GHG} = P_\alpha + f_1 P_\alpha \quad (7)$$

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where  $P_\alpha = S_0 \{0.25x(1 - Albedo)\}$  and  $S_0 = 1361 \text{ W/m}^2$ . The equilibrium model is constrained by the energy balance discussed in Section 2.4 and 2.6.

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In 2019 due to global warming trends, this model is more complex and harder to separate out terms. However, it can still be done looking at a snapshot point in time using equilibrium theory, so

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$$P_{Total2019} = P_{\alpha'} + P_{GHG'+Feedback} = P_{\alpha'} + f_2 P_{\alpha'} \quad (8)$$

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Here,  $P_{GHG'+Feedback}$  includes GHGs and its increase including water-vapor, lapse rate effect and other changes such as an increase in snow-ice albedo variations that are hard to separate out. That is, some of this feedback is related to GHG forcing increases and some is related to albedo change.  $P_{\alpha'}$  represents the 2019 albedo due to changes in UHI absorption, cloud absorption, ice and snow melting, and so forth that can be discerned. We note that  $f$ , a measure of the emissivity, is **not** constant but must change since the amount of GHGs change.

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However the re-radiation still must connect the absorption to re-radiation. We use a linear  $f$  parameter that indicates the fraction of  $P_\alpha$  power that must be re-radiated back to obtain the observed temperature. To be clear,  $f$  is just a fractional parameter related to the emissivity. In 1950 it was some function of the GHGs (with no feedbacks). In 2019, it is more complex. The model is also constrained relative to  $f_1$  as described in Section 2.6. However, it is primarily related to GHGs re-radiation since  $P_{GHG} \approx P_{GHG'+Feedback}$ .

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115 **2.3 Balancing  $P_{out}$  and  $P_{in}$**

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117 Although Eq. 7 is reasonably simple,  $f_1$  has the uniquely defined value found in Eq. 6. This should also result from  
118 balancing the energy in and out of our global system.

120 **2.3.1 Balancing  $P_{out}$  and  $P_{in}$  in 1950**

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122 To balance the energy in with the energy out in 1950 with no global warming imbalance we can still start with Eq. 7.  
123 In equilibrium the radiation that leaves must balance what comes in  $P_\alpha$  so that

124  
125 
$$\begin{aligned} Energy_{Out} &= (1-f_1)P_\alpha + (1-f_1)P = (1-f_1)P_\alpha + (1-f_1)\{P_\alpha + f_1P_\alpha\} \\ &= (1-f_1)\{2P_\alpha + f_1P_\alpha\} = 2P_\alpha - f_1P_\alpha - f_1^2P_\alpha = Energy_{In} = P_\alpha \end{aligned} \tag{9}$$

126  
127 In 1950, the value  $f$  solves the quadratic equation as found in Eq. 6

128  
129 
$$f_1^2 + f_1 - 1 = 0 \text{ yielding } f_1 = 0.618 \tag{10}$$

130  
131 Interestingly, this also says that

132  
133 
$$P_\alpha = f_1 P_{Total\_1950} \text{ or } P_\alpha = f_1(P_\alpha + f_1P_\alpha) \text{ or } 1 = f_1(1 + f_1) \tag{11}$$

134  
135 The RHS of Eq. 11 is Eq. 10 and Eq. 6. This illustrates why  $f_1$  is unique. It is the fractional amount of total radiation  
136 that is in equilibrium. As a final check, results will show in Section 3 and Table 1, that the value  $f_1$  provides  
137 reasonable results.

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139 **2.3.2 Warming Imbalance in 2019**

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141 The re-radiation parameters  $f_1$  and  $f_2$ , are connected and from Eq. 7 and 8 we have

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143 
$$f_2 = f_1 + \left(\frac{P_{2019}}{P_{\alpha'}} - \frac{P_{1950}}{P_\alpha}\right) = f_1 + \Delta f \tag{12}$$

144 In this way  $f_2$  is a function of  $f_1=0.618$  and the differences in the global warming residuals that is identified in Eq. 12  
145 as  $\Delta f$ .

146  
147 **3.0 Results and Discussion**

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149 Since the re-radiation parameter is fixed for  $f_1=0.618$ , to obtain  $T_{1950}=13.89^\circ\text{C}$  ( $287.038^\circ\text{K}$ ), the only adjustable  
150 parameter left in our simple model is the Earth's albedo. This value requires an albedo value of 0.3008 (see Table 1)  
151 to obtain the correct value  $T_{1950}$ . This albedo numbers is reasonable and similar to values cited in the literature [4].

152  
153 In 2019, the average temperature of the Earth is  $T_{2019}=14.84^\circ\text{C}$  ( $287.99^\circ\text{K}$ ). Here we are not sure of the albedo since  
154 it likely changed due to UHI increase, snow and ice melting and cloud coverage changes. The IPCC value in AR5  
155 [5] is 0.294118. However, this would represent a 3% change since 1950 which may be an overestimation. In our  
156 assessment, we will assume a 1% change. Then, the  $f_2$  parameter is adjusted to 0.6324 to obtain  $T_{2019}$ . Results are  
157 provided in Table 1. The results yield  $P_{Total\_1950}=384.935 \text{ W/m}^2$  and  $P_{Total\_2019}=390.055 \text{ W/m}^2$ . We find that

158 
$$\Delta P_{Total} = P_{2019} - P_{1950} = 5.121 \text{ W/m}^2 \tag{13}$$

159 and

160 
$$\Delta T_{Total} = T_{2019} - T_{1950} = 0.95^\circ\text{C} \tag{14}$$

161  
162 which is the observed surface temperature increase since 1950.

163  
164 **Table 1** Model results

Year	T( $^\circ\text{K}$ )	T $_\alpha$ ( $^\circ\text{K}$ )	$f_1, f_2$	$\alpha, \alpha'$	$P_\alpha, P_{\alpha'}$ ( $\text{W/m}^2$ )	$P_{GHG}$ ( $\text{W/m}^2$ ) $P_{GHG'+feedback}$	$P_{Total}$ ( $\text{W/m}^2$ )
2019	287.991	254.78	0.63253	29.779	238.927	151.128	390.055
1950	287.041	254.51	0.6180	30.08	237.903	147.032	384.935
$\Delta 2019-1950$	<b>0.95</b>	0.27	<b>1.45%</b>	-0.3 <b>(1%)</b>	<b>1.024</b>	4.096	<b>5.121</b>

166 Table 1 summarizes model results for the specified albedos and observed Earth's surface temperatures. To show  
 167 model consistency, the forcing change  $5.121 \text{ W/m}^2$ , resulting in a  $0.95^\circ\text{K}$  rise, should agree with what is expected  
 168 from Planck's feedback parameter. From Eq. A-1, it is evident that

$$170 \quad \beta^4 \Delta R_{\text{TOA}} = 5.097 \times \beta^4 = 3.165 \text{ W/m}^2 \quad (15)$$

171 This equation illustrates the consistency of the simple re-radiation model. Then, Planck's feedback parameter ( $3.3$   
 172  $\text{W/m}^2/^\circ\text{K}$ ) temperature rise is in agreement with what is observed by equilibrium modeling

$$175 \quad 3.165 \text{ W/m}^2 \times (1/3.3)^\circ\text{K/W/m}^2 = 0.959^\circ\text{K at } T_s \quad (16)$$

### 177 3.1 Why the Re-radiation Parameter is Significant

178 In Table 1, the measure of  $\Delta f = 1.45\%$  fractional increase is due to re-radiation change. This is significant. From Eq.  
 179 7, 8 and 12 we can illustrate this key characteristic of climate change

$$182 \quad \Delta f = \left( \frac{P_{2019}}{P_{\alpha'}} - \frac{P_{1950}}{P_{\alpha}} \right) = \left( \frac{P_{GHG'+F}}{P_{\alpha'}} - \frac{P_{GHG}}{P_{\alpha}} \right) \approx \left( \frac{P_{GHG'+F} - P_{GHG}}{P_{\alpha}} \right) \quad (17)$$

183 Therefore,  $f$  is an estimate of climate re-radiation and  $\Delta f$  an estimate of climate emissivity change. It is a measure of  
 184 GHG forcing increase and the feedback relative to the initial 1950 radiation, and is generally helpful in looking at  
 185 how our climate is working. Furthermore, we can deduce an albedo advantage.

### 188 3.2 The Albedo Advantage

189 We can look at an important ratio, the power created by the albedo effect compared to GHGs in 1950. The initial  
 190 radiation is  $P_{\alpha}$  which heats the Earth to  $254.51^\circ\text{K}$ , and then according to Eq. 7 and Table 1, the  $P_{GHG}$  energy  
 191 originates from a fraction of this original heating due to re-radiation as  $fP_{\alpha}$

$$194 \quad \frac{P_{\alpha} + P_{GHG}}{P_{GHG}} = \frac{P_{\alpha} + fP_{\alpha}}{P_{GHG}} = \frac{P_{\alpha} + fP_{\alpha}}{fP_{\alpha}} = \frac{1 + f_1}{f_1} = \frac{1.62}{0.62} = 2.62 \quad (18)$$

195 Again this is a key difference in how other authors look at the albedo effect [1] and short wavelength absorption.  
 196 Here we include the re-radiation that must occur from short wavelength absorption. In general, this also means that  
 197 albedo change has a higher impact factor in climate forcing, 2.6 times larger than  $\Delta P_{GHG}$  as well, that is a change,  
 198  $\Delta P_{\alpha}$  compared with a change in  $\Delta P_{GHG}$  would yield the same impact factor  $d(P_{\alpha} + P_{GHG}) = 2.62 d(P_{GHG})$  or assuming  
 199  $\Delta f \ll 1$

$$201 \quad \frac{\Delta P_{\alpha} + \Delta P_{GHG}}{\Delta P_{GHG}} \approx \frac{\Delta P_{\alpha} + f \Delta P_{\alpha}}{f \Delta P_{\alpha}} \approx \frac{1 + f_1}{f_1} = \frac{1.62}{0.62} = 2.62 \quad (19)$$

202 This is a key reason that UHIs, cloud coverage, snow, and ice melting, can create significant climate effects.  
 203 Appendix B puts this important impact factor in plain language. We see this is a different kind of comparison then  
 204  $\lambda_{GHG}/\lambda_{\alpha}$ . It uses a re-radiation parameter obtained mainly from the equilibrium model.

205 In this view, an albedo solution is advantageous having significant potential for reversing global warming or  
 206 ignoring it, as in UHIs likely can create serious issues. Therefore, trying to control global warming by reducing  
 207 GHGs is important. However, certainly, an albedo approach is even more advantageous. It reduces both initial  
 208 absorption and its potential for its re-radiation. Its impact rating can be taken as 162% compared to re-radiation  $f$   
 209 with a 62% impact by comparison according to Eq. 18 and 19, yielding a 2.6 times higher advantage. It is important  
 210 to realize that because the albedo solution can highly impact global warming and reverse trends, it is also vital in  
 211 preventing a tipping point from occurring.

### 215 3.3 Planck-Albedo Parameter

216 The albedo changes and  $\Delta P_{\alpha}$  in Table 1, are:  $\% \Delta \alpha = 1\%$  and  $1.024 \text{ W/m}^2$ , respectively. We note that we can define a  
 217 unique Planck-albedo parameter  $\lambda_{\% \Delta \alpha} = \Delta P_{\alpha} / \% \Delta \text{albedo}$ . To illustrate from Table 1

$$220 \quad \lambda_{\% \Delta \alpha} = 1.024 \text{ W/m}^2 / \% \Delta \text{albedo} = 1.024 / 1\% \quad (20)$$

221 This parameter can also be expressed per degree (noting the  $0.95^\circ\text{K}$  change in Table 1)

$$\lambda_{\% \Delta \alpha \Delta T} \approx 1W / m^2 / \Delta \% albedo / ^\circ K \quad (21)$$

225  
226 The parameter was first noted in Feinberg 2020 [3] but is featured here as a modeling tool. We term it the Planck-  
227 albedo parameter, since it relates to blackbody ( $P_\alpha$ ) absorption. A simple numeric example is given in the conclusion  
228 to illustrate how it provides helpful estimates. This interesting parameter arises from the basic assessment of the two  
229 equilibrium time periods

$$\lambda_{\% \Delta \alpha} = \frac{(\Delta E_o)_\alpha}{\alpha_1 - \alpha_2} \frac{1}{100} = \frac{E_o (\alpha_1 - \alpha_2)}{\alpha_1 - \alpha_2} \frac{1}{100} = E_o \alpha_1 / 100 \approx 1W / m^2 / \% \Delta albedo \quad (22)$$

231 where  $E_o=340 \text{ W/m}^2$  and when  $\alpha_1$  is 29.4118%, the value  $1.000\text{W/m}^2/\Delta \% albedo$  is obtained. We note the value  
232 29.4118% (100/340) is given in AR5 [6]. The parameter's relationship to  $\lambda_\alpha$  is

$$\lambda_\alpha = \lambda_{\% \Delta \alpha \Delta T} x \% \Delta \alpha \quad (23)$$

236 and the feedback parameter could including re-radiation factor  $f$  in 2019 [2] as

$$\lambda_\alpha^\dagger = \lambda_{\% \Delta \alpha \Delta T} x \% \Delta \alpha x 1.618 \quad (24)$$

#### 240 4.0 Conclusion

241 In this paper, we provided a simple re-radiation global warming model. The model shows consistency with the  
242 Planck parameter. We noted that the re-radiation parameter increased by about 1.45% due to global warming from  
243 1950 to 2019, illustrating the warming from a different perspective. From the model, the albedo effect was  
244 quantified, having an impact rating of 162% compared to GHGs with 62%. The albedo effect then yields a 2.6 times  
245 higher advantage upon comparison. These results strongly support moving forward with solar geoengineering  
246 solutions [3, 7-9].

249 We also found a handy parameter that we termed the Planck-albedo parameter, which is about  
250  $\lambda_{\% \Delta \alpha \Delta T} \approx 1W / m^2 / \Delta \% albedo / ^\circ K$ . This finding can be helpful in quickly estimating the effect of an albedo change on  
251 global warming and in assessing  $\lambda_\alpha$ . For example, Feinberg 2020 [2] suggested a goal of 1.5% geoengineering  
252 albedo change. Using this parameter, an impact of -1.5 Watts/m<sup>2</sup> warming reduction should result. Given a 1.62  
253 reemission factor (Eq. 18), this is -2.4 W/m<sup>2</sup> improvement. With a decrease in water-vapor feedback, often estimated  
254 by a factor of 2 [10], provides a resulting overall effect that could be as high as -4.8 W/m<sup>2</sup>. One can compare this to  
255 the 5.12 W/m<sup>2</sup> results in Table 1 indicating a significant resolution to the current warming trend. Feasibility is  
256 discussed in more detail in Feinberg's 2020 paper [2] and other solutions have been proposed [7-9].

#### 258 Appendix A

##### 260 Overview of Planck Feedback Parameter

262 Estimates on Planck's feedback parameter are varied, typically between -3.8W/m<sup>2</sup>/°K and -3.21W/m<sup>2</sup>/°K with some  
263 values as large as -7.1W/m<sup>2</sup>/°K [11]. The IPCC AR4 [12] lists a value of -3.21W/m<sup>2</sup>/°K. Numerous authors have  
264 developed different expressions [11]. A typical estimate starts with

$$F_{TOA} = (1 - \alpha) S_o / 4 - \sigma (\beta T_s)^4 = (1 - \alpha) S_o / 4 - R_{LWR} \quad (A-1)$$

268 where  $S_o=1361 \text{ W/m}^2$ ,  $F_{TOA}$  is the radiation budget at the top of the atmosphere,  $R_{LWR}$  is the outgoing long wave  
269 radiation (a function of surface temperature and albedo),  $\sigma$  is the Stefan-Boltzmann constant and  $\beta$  is described in  
270 this section below and later will be redefined in terms of a re-radiation parameter. Then the Planck parameter  $\lambda_o$  can  
271 be calculated as

$$\lambda_o = \partial F_{TOA} / \partial T_s = -\partial R_{LWR} / \partial T_s \quad (A-2)$$

275 This result is

$$\lambda_o = -4\beta^4 \sigma T_s^3 = -4\beta \sigma T_{TOA}^3 \quad (A-3)$$

279 where  $\beta$  varies in the literature from 0.876 to 0.887 (averaging=0.8815) and  $T_s=288^\circ\text{K}$  [12]. This yields -  
280  $3.37\text{W/m}^2/^\circ\text{K} < \lambda_o < -3.21\text{W/m}^2/^\circ\text{K}$ . However, from Eq. A-3,  $\beta$  is often taken as the ratio

$$\beta = T_{TOA} / T_s = 255^\circ K / 288^\circ K = 0.8854 \text{ and } \beta^4 = 0.615 \quad (\text{A-4})$$

283  
284 A common assessment uses  $T_{TOA}=255^\circ K$ , so that  $\lambda_o = -3.33 W/m^2/^\circ K$ . Another expression developed by Schlesinger  
285 [6] is dependent on the albedo and surface temperature as

$$\lambda_o = S_o (1 - \alpha) / T_s \quad (\text{A-5})$$

288  
289 When  $S_o=1361$ ,  $0.294118 < \alpha < 0.3$ , and  $T_s=288^\circ K$  then  $-3.308 W/m^2/^\circ K > \lambda_o > -3.3358 W/m^2/^\circ K$ , respectively.

### 291 *A.1 Estimating Planck's Parameter with an Albedo Method*

292 Consider a global albedo change corresponding to  $1^\circ K$  rise from solar absorption letting

$$F_{TOA} = 0 = (1 - \alpha) E_o - \sigma (T_s)^4 \quad (\text{A-6})$$

296 where  $E_o = S_o/4$ . Then a  $1^\circ K$  change is

$$\Delta T_s = T_2 - T_1 = \left( \frac{E_o}{\sigma} (1 - \alpha_2) \right)^{1/4} - \left( \frac{E_o}{\sigma} (1 - \alpha_1) \right)^{1/4} = 1^\circ K \quad (\text{A-7})$$

299 Here we will use the AR5 albedo starting value of 0.294118 [6]. We find that the corresponding albedo change is  
300 0.28299 when  $E_o=340 W/m^2$ . This corresponds to

$$\Delta E_o = E_o \{ (1 - \alpha_2) - (1 - \alpha_1) \} = E_o (\alpha_1 - \alpha_2) = 3.784 W / m^2 \quad (\text{A-8})$$

304 Since this is for a  $1^\circ K$  rise, then it can also be written as

$$\lambda_{1K} = 3.784 W/m^2/^\circ K \quad (\text{A-9})$$

309 We note this is related to the surface value, then

$$\lambda_{1K} = -4\sigma T_s^3 \quad (\text{A-10})$$

311 By comparison to above we have

$$\lambda_o = \lambda_{1K} \beta = -3.784 W/m^2/^\circ K = -3.349 W/m^2/^\circ K \quad (\text{A-11})$$

314 This is very close to the  $-3.33 W/m^2/^\circ K$  value obtained in the traditional manner.

### 316 *A.2 Top of the Atmosphere and Beta*

317 From Eq. A-1

$$R_{LWR} = \sigma (\beta T_s)^4 = \sigma (T_{TOA})^4 \quad (\text{A-13})$$

321 giving

$$\beta^4 R_{TOA,T_s} = R_{TOA,T_{TOA}} \quad (\text{A-14})$$

324 We will need this expression later when showing model consistency with the Planck feedback parameter.

## 327 **Appendix B**

329 Plain Language - Quantifying the Albedo Advantage

330  
331 It may be helpful for the reader to have a layman's view of the 2.62 factor. Consider the Earth with a roof. The roof  
332 represents the GHGs over the Earth and only allows 40% of any energy leaves with the rest returning to Earth.  
333 Sunlight comes in, and some is absorbed and heats the Earth's floor to  $255^\circ K$  ( $-2.3^\circ F$  very cold). Let's say it takes  
334 100 units of energy. The heat rises, but only 40 units of energy can leave from the roof, so 60 units come back and  
335 warms the Earth's floor to  $288^\circ K$  ( $57^\circ F$  average temp of Earth). On average, the Earth's floor is heated by a total of  
336 160 units. The sun keeps warming the Earth's floor at 100 units on average, and the roof keeps sending back 60  
337 units. So the roof is responsible for 60 units on average of energy, and the Earth's floor is warmed by 160 units on  
338 average. We can write this as

- 339  
340 • Energy units:  $160 = 100 + 60 = 100 + 100 \times 0.6$

341 We see the 100 units are in two places in the equation due to the floor and roof, while 60 units is only in one place.  
 342 That is without the floor absorption first, the roof cannot keep the Earth warm. Therefore, the heat coming from the  
 343 Earth's floor results in 160 units and the roof is only 60 units by comparison. The impact factor is  
 344

- 345 •  $160/60=2.66$ , that is, the heat from the Earth's floor has this much larger impact.

346 Alternately, for every unit of energy given off, by the Earth's floor after absorption it is equivalent to causing 1.6  
 347 units of heating while the roof (GHG) is only responsible for 0.6.

348 How much heat leaves in equilibrium? Of the 100 units of energy absorbed and radiated, the initial 40 units left. As  
 349 well, the Earth's floor received a total of 160 units, but the roof only let 40% leave that's another 64 ( $=0.4 \times 160$ )  
 350 units of energy leaving. The total leaving is 104 units in equilibrium, so roughly 100 units comes in and almost same  
 351 goes out.

352 This estimate can be refined to 61.8% (Eq. 20). Then, 100 units are absorbed and radiated, so 38.2 units initially  
 353 leave, and 61.8 units is re-radiated to the Earth's floor which is now heated to 161.8 units of energy. From this  $0.382$   
 354  $\times 161.8$  leaves=61.8 units or energy. The total is  $61.8+38.2=100$  units of energy leaves and another 100 units,  
 355 establishing equilibrium. Any eventual difference causes global warming.

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