

Dark Matter is Negative Mass

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There has been an old and false claims in the scientific community related to negative mass. This paper describes the vacuum instability problem, runaway motion problem, and wheel problem with negative mass and positive mass. Negative mass is an object whose existence is required by the law of the conservation of energy. The fundamental properties of negative mass can explain important characteristics of dark matter. 1) additional centripetal force effects, 2) explanations derived from fundamental principles about the reason why dark matter does not have electromagnetic interaction, 3) repulsive gravity ensuring almost even distribution and lower interaction of dark matter, 4) gravitational lens effect, 5) accelerating expansion of the universe can be explained with negative mass. Therefore, we should seriously examine the negative mass model.

I. Introduction

The dark matter had been reported by Fritz Zwicky, 1933, [1] [2] and then was rediscovered by Vera Rubin and Kent Ford, 1979. [3] Since then, it has emerged as one of important issues in the academic world.

There have been a lot of articles on the dark matter, a very important issue regarding the formation of galaxy and evolution of the universe. [4] [5] Therefore, this paper does not explain such things, but will focus on the negative mass model.

1. Brief current conditions of dark matter candidates

1) WIMP succeeds in rough explanations by combining with Cosmological Constant Λ , [4] [5] but fails in the direct detection experiment. [6–8] Moreover, it also fails in production with LHC, a completely different approach. [9] [10]

2) Until now, supersymmetry particles have not been detected from LHC [9] [10] and the evidence that 4th neutrino exists has not been found by observation of the Plank satellite. [11]

3) The MOND theory usually requires fine tuning of each galaxy, [12] has difficulty explaining Bullet Cluster [13] and collides with many observational evidences of the dark matter. [4] [5]

II. Main Characteristics of Negative Mass

Some phenomena of relativity and quantum mechanics are against common sense. Already, accelerating expansion of universe is not what we expected. [14] [15] The rotation curves of galaxies were not what we expected. It is a phenomenon that conflicts with common sense in some aspects.

Already, an uncommon event has occurred. In this situation, what you need to focus on is not your common sense but does the newly introduced physical quantity explain the phenomenon?

1. Negative mass has both negative inertial and gravitational mass. [16]

The motion characteristics of negative mass have been fully explained in the previous papers [17–19], so please refer to the paper and the following video. [20]

One thing to note in the discussion is that the terms that have already been applied to positive masses can be confusing.

There are repulsive gravitational effects between negative masses.


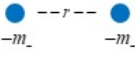
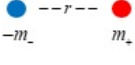
	Force	Motion	Active Mass
	$F_{++} = -\frac{Gm_+m_+}{r^2}$ Attraction or attractive force	Attractive motion or attractive effect (decrease in distance)	$F = -\frac{Gm_+(_)}{r^2}$ Attract
	$F_{--} = -\frac{G(-m_-)(-m_-)}{r^2} = -\frac{Gm_-m_-}{r^2}$ Attraction or attractive force	Repulsive motion or repulsive effect (increase in distance)	$F = -\frac{G(-m_-)(_)}{r^2}$ Repel
	$F_{-+} = -\frac{G(-m_-)(+m_+)}{r^2} = +\frac{Gm_-m_+}{r^2}$ Repulsion or repulsive force	$-m_- < m_+$: Attractive motion (decrease in dist.) $-m_- = m_+$: Runaway motion $-m_- > m_+$: Repulsive motion (increase in dist.)	

Figure 1: Different forms of explanation based on criteria(Force, Motion, Active Mass). Due to the negative inertial mass, the direction of force and motion changes.

One of problems regarding movement of negative mass, which researchers are likely to misunderstand is that if there are negative mass particles around the earth (or galaxy), large positive mass, they may not fly to the universe, but freely fall to the earth (or galaxy). Thus negative masses are clustered outside galaxy or cluster of galaxies. [18]

2. See the following video produced to help understand movement of negative mass.

<http://www.youtube.com/watch?v=MZtS7cBMic4> [20]

3. Positive mass is stable at the low energy state, while the negative mass is stable at the high energy state. [17] [18]

One of physics' fundamental principles, "lower energy state is associated with stability" can be only applied to positive mass. However, both negative mass and negative energy level have been denied, as it has been wrongly applied to negative mass.

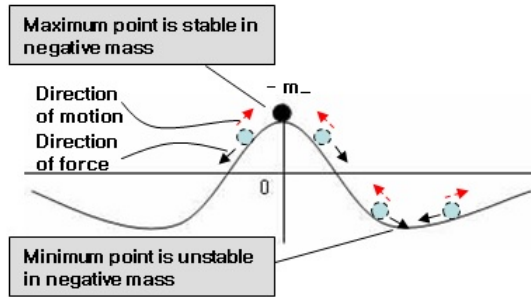


Figure 2: When there is negative mass in potential which has a point of maximum value and a point of minimum value.

$$\vec{F} = -m_- \vec{a} \quad (m_- > 0) \quad (1)$$

$$\vec{a} = -\frac{\vec{F}}{m_-} \quad (2)$$

When negative mass exists within potential with maximal and minimal points, different directions of force and acceleration should be considered for negative mass.

The acceleration of negative mass is opposite to the direction of force. Therefore, the negative mass has harmonic oscillation at the maximum point and it is also stable at the maximum point.

In the case of positive mass, it was stable at the minimum point at which energy is the low. However, in case of negative mass, stable equilibrium is a point of maximum value, not a point of minimum value.

It is stable at a low energy state in the case of positive mass. However, it is stable at a high energy state in the case of negative mass. Due to this, “the problem of transition to minus infinite energy level” does not occur, therefore negative mass(energy) and positive mass(energy) can exist stably in our universe. [17] [18]

4. False claims about negative mass

1) The vacuum instability problem is wrong. [18] [19]

In case of a positive mass, it could have negative energy level within negative potential. Nevertheless, even in this case, the total energy containing potential energy was still in the state of positive energy.

However, for positive mass to enter the domain of (total energy is negative) negative energy level, energy should have negative value, and this means that it should have the characteristics of negative mass.

When considering the process of entering into the domain of negative energy levels from positive energy levels, it must pass through the domain between 0^- (Approach from negative direction to ‘0’) and $-\frac{1}{2}\hbar\omega$ (corresponds to a certain negative energy level). In the case that it follows the laws of negative mass because it is in the domain of negative energy, it cannot reach $-\frac{1}{2}\hbar\omega$, which is the first negative energy level, because it is stable at the state of high energy and it tries to have higher value of energy.

This is because the energy level 0^- is much higher than the energy level $-\frac{1}{2}\hbar\omega$. Thus, this implies that the law of negative mass itself does not allow a situation where positive mass at the positive energy level transitions to the negative energy level.

Even if it reaches $-\frac{1}{2}\hbar\omega$, it is most stable state for negative mass and “the problem of the transition of the energy level of minus infinity” does not occur.

As we have examined above, “the problem of the transition of the energy level of minus infinity” does not occur, and thus positive mass and negative mass can exist in the same space-time. This is a very important result because it means that negative mass and negative energy can exist stably in our universe.

2) The runaway motion problem is wrong.

Runaway motion is an argument that the two masses continue to accelerate, in an ideal situation where the negative mass and the positive mass are exactly the same. [16] Runaway motion is used as a rejection logic of negative mass because no large energy motion is observed. [21]

a) The difference in mass when creating the pair of negative mass and positive mass [18]

As a general conjecture, when positive and negative mass are born, the mass will be exactly the same, but this conjecture is wrong. There is at least a gravitational potential energy between the two particles.

In the process of the pair creation of electron and positron, the effect of electromagnetic potential energy could be the same because the two particles had the same kind of energy(electron : +, positron : +). Therefore, the two particles could have the same mass. However, in the process of the pair creation of negative and positive mass, the effect of gravitational potential energy is different because the two particles have different types of energy(negative mass : -, positive mass : +).

This gravitational potential energy has a positive value and exists in a system containing two objects or two objects. If you add or subtract potential energy in two cases(Pair creation of electron and positron, Pair creation of negative mass and positive mass), you can see that they are different.

$$m_- > 0, m_+ > 0$$

$$E_T = 0 = (-m_-c^2) + (+m_+c^2) + \frac{Gm_+m_-}{r} = 0 \quad (3)$$

$$m_- = m_+ + \frac{Gm_+m_-}{rc^2} \quad (4)$$

In case the negative mass and the positive mass are pair created in the vacuum, according to the Energy Conservation Law, there must be a mass difference between the negative mass and the positive mass. [18]

$$|-m_-| > m_+ \quad (5)$$

As described in the previous paper [18] [19], acceleration is determined by the size of the opponent's mass. If the absolute value of the negative mass is greater than the absolute value of the positive mass, there is a repulsive gravitational effect between the two. In this case, the acceleration of positive mass is greater. As time passes, the two masses become more and more distant. In other words, the ideal situation of pairing is broken. Because the accelerations are not the same and the distance of the pairing increases, the interaction of the other particles becomes involved. Therefore, runaway motion is not maintained. In the classical analysis, the larger the mass difference(The shorter the distance of a pair), the more easily the pairing breaks.

This logic may be used as a theoretical basis(energy conservation law, mass difference, repulsive gravitational effect) for the presence of two masses after pair creation without pair annihilation. Please watch($|-m_-| > m_+$ case) the linked video. [20]

b) There is a possibility that the gravitational potential energy will break the ideal situation.

Although the absolute values of the masses of two objects are exactly the same, there is a gravitational potential energy between them.

$$U = -\frac{G(+m)(-m)}{r} = +\frac{Gmm}{r} > 0 \quad (6)$$

This gravitational potential energy has a positive value and exists in a system containing two objects or two objects. And, since all energy is a source of gravity, the gravitational potential energy must also act gravity source.

Thus, these experiments indicate that gravitational energy gravitates in the normal way. [22]

That is, even if the masses of negative mass and positive mass are exactly the same, the gravitational potential energy between them breaks this ideal situation.

c) Since “runaway motion” assumes a very ideal situation, an unusual movement occurs, but in the real world, this ideal situation may be broken by external factors (forces or fields by other objects . . .)

d) The possibility that the pair creation of a mass of negative and positive occurred only in the early part of the universe.

In the present time, there is a possibility that there will be limited pair creation as fields(electromagnetic field, strong field, weak field) exist.

3) The wheel problem is wrong. [23]

Regarding the negative mass, the following argument has long been in the academic world. However, this claim is also completely wrong.

What happens if one attaches a negative and positive mass pair to the rim of a wheel? This is incompatible with general relativity, for the device gets more massive.

-Thomas Gold, in *Negative mass in general relativity* [24]

a) In terms of force [23]

There is a problem of “How do you combine a negative mass with a rod?” But let's assume that it is connected in any way. The forces acting on both rods are equal in magnitude and opposite directions.

$$\vec{F}_L = -\vec{F}_R \quad (7)$$

Therefore, the wheel does not rotate.

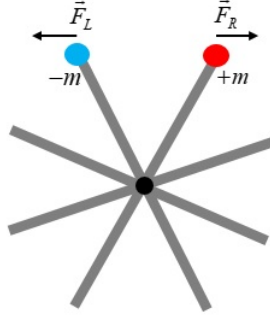


Figure 3: When the negative and positive mass is attached to the end of the wheel. In terms of force

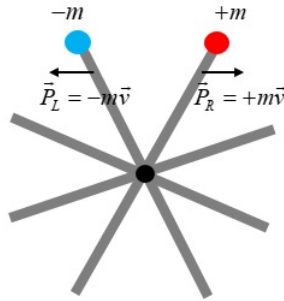


Figure 4: When the negative and positive mass is attached to the end of the wheel. In terms of momentum

b) In terms of momentum [23]

In order for the wheel to move, momentum must be transmitted to the rod. But,

$$\vec{P}_L = -\vec{P}_R \quad (8)$$

The momentum transmitted to both rods is completely canceled. Therefore, the wheel does not rotate. He should have thought that the momentum had to be transmitted in order for the wheel to rotate.

5. Resurrection Request for Negative Mass.

All new discoveries were called new discoveries because they were not found until then. Throughout the history of science, among the things that have not yet been discovered, new discoveries have had many examples. In other words, it does not guarantee that undiscovered findings of any physical object will be undiscovered in the future. The history of physics, and even the history of science.

And even if we find something, our existing knowledge either rejects this discovery or tries to interpret it only through existing ideas.

In 1998 observations, the first result of the Friedmann equation was negative mass density. But the researchers, who had difficulty accepting negative masses, modified the equation. And they argue that the accelerated expansion of the universe is evidence of the existence of a cosmological constant. [14] [15] New ideas that challenge the paradigm are hardly subject to legitimate scientific review. In the process of discarding the negative mass that is the result of the field equation, it is assumed that the false claims listed above played a key role. Since the rejection logics for the negative mass are wrong, the negative mass model needs to be reviewed again.

From the second Friedmann equation or acceleration equation,

$$\frac{1}{R} \left(\frac{d^2 R}{dt^2} \right) = - \left(\frac{4\pi G}{3} \right) (\rho + 3P) \quad (9)$$

Since ρ is the energy density in the acceleration equation, the pressure term P also has a dimension of energy density ($c=1$). Current acceleration equation inevitably require negative (gravitational) mass density. Without negative (gravitational) mass density, it is impossible to create acceleration expansion. The mainstream produces acceleration expansion by setting the pressure of the cosmological constant or vacuum energy to $P = -\rho$. [25]

However, the notion (dark energy term) created by the mainstream has an inertial mass density of $+1(\rho)$, equivalent mass density of kinetic energy (or negative pressure) of $-3(\rho)$, with gravitational mass density of $-2(\rho)$. Not only different signs, but different values. It violates the principle of equivalence of inertial mass and gravitational mass, which is the basis of general relativity theory.

Looking at the dark energy term,

$$-2\rho = \rho + 3(-\rho) = -2\rho \quad (10)$$

a) Sign of the negative pressure

In the acceleration equation, $3P$ has the idea of an equivalent mass density corresponding to the kinetic energy of the particle. So, assuming that the pressure P term has a negative energy density is same assuming that it has negative kinetic energy. In order to have negative kinetic energy, it must have negative inertial mass. But, because they assumed a positive inertial mass, it is a logical contradiction.

b) Size of the negative pressure

In the ideal gas state equation, we obtain,

$$P = \frac{1}{3} \left(\frac{v^2}{c^2} \right) \rho = \omega \rho \quad (11)$$

In the case of mater, $v \ll c$, $\omega = 0$, In the case of radiation, $v = c$, $\omega = \frac{1}{3}$

By the way, how can we physically create three times ω larger than light? How do we get the size 1 of $|\omega|$? If we assume an object with superluminal speed $\sqrt{3}c$, can we explain it? Well, we can avoid this problem by assuming that cosmological constant or vacuum energy does not apply to the results (ideal gas state eq.) obtained through physics. However, ideal gas state equation applies to “massless to infinite mass” particles, and the velocity ranges from “0 to c ” are all included. If we seriously consider the physical presence of $P = -\rho = -3(\frac{1}{3}\rho)$, we will find that there is a serious problem.

The relation $P = -\rho$ obtained from thermodynamics is obtained from the assumption that the energy density is constant even when the space expands. This conclusion is only a conclusion obtained by assuming certain conditions hold, and may not guarantee the existence of a physical reality.

[(Simple) Negative mass model]

Inertial(Gravitational) mass density : $-2(\rho)$,

[Mainstream model]

Inertial mass density : $+1(\rho)$,

Equivalent mass density of kinetic energy (or pressure term) : $-3(\rho)$

Gravitational mass density : $-2(\rho)$.

We have to know that not the field equation has disposed the negative mass, but our wrong stereotype disposed that negative mass.

III. Dark Matter is Negative Mass

1. Negative mass is an object whose existence is required by the law of the conservation of energy. [18] [19]

If the conservation of energy that “energy will be always conserved” is applied to the initial state of the universe, this gives rise to the question of “where the energy of our universe did come from?”. The most natural answer to this question is the assumption that the energy itself was not something created and that zero-energy

state went through phase transition keeping conservation of energy and generating negative and positive energy. Therefore, in order to offset the known positive energy of matter, negative energy is needed.

Edward Tryon, Stephen Hawking, Alan Guth, and Alexander Vilenkin are the pioneers who advocated that positive mass energy could be offset by gravitational potential energy. [26] However, there model has some disadvantages.

First, it is possible for the negative gravitational potential energy to offset the positive mass energy. By the way, looking for the size in which total gravitational potential energy becomes equal to total rest mass energy by comparing both, [27] [28]

$$U_{gs} = \left| -\frac{3}{5} \frac{GM^2}{R_{gs}} \right| = Mc^2 \quad (12)$$

$$R_{gs} = \frac{3}{5} \frac{GM}{c^2} \quad (13)$$

Comparing R_{gs} with R_S , the radius of Schwarzschild black hole,

$$R_{gs} = \frac{3}{5} \frac{GM}{c^2} < R_S = \frac{2GM}{c^2} \quad (14)$$

$$R_{gs} = 0.3R_S \quad (15)$$

This means that there exists the point where gravitational potential energy becomes equal to mass energy within the radius of black hole, and that, supposing a uniform distribution, the value exists at the point $0.3R_S$, a 30% level of the black hole radius. [27] [28] If the virial theorem holds, then $R_{gs} = 0.15R_S$. In other words, in order for there model to be established, our universe must exist in a black hole. For some people, this is a problem.

Second, the universe is expanding.

The universe is expanding. Mass term $+Mc^2$ is constant, whereas R increases, and so the absolute value of gravitational potential energy $\left| -\frac{3}{5} \frac{GM^2}{R} \right|$ gets smaller and finally energy state of 0 is broken. In general, the kinetic energy is small compared to the mass energy and can be ignored. And, it's a positive energy. [29]

To look at how equation is valid by unfolding the formula,

$$Mc^2 - \frac{3}{5} \frac{GM^2}{R} = 0 \quad (16)$$

$$M = \frac{5c^2}{3G} R \quad (17)$$

In their model, to establish energy conservation law (zero energy state) while the universe is expanding, energy needs to be increased, which increases R of the universe. [29] This is a fatal problem.

At present, the gravitational potential energy does not completely offset mass energy. And for the birth of the universe from “nothing or zero energy” and energy conservation at the birth of the universe, negative mass, which corresponds to negative energy, is of utmost necessity. The negative mass is the demand and outcome of the law of conservation of energy.

2. Negative energy does not have positive energy to produce charges, so is unlikely to have electromagnetic interaction.

Think about whether negative mass has charges.

It is possible that the model designer assumes two models of negative mass with and without charges. However, let's infer what a state is more proper, based on the existing physical laws.

We have observed pair production due to the collision of photon with atomic nucleus. Such phenomena suggest that the process of pair production exists where the charge Q does not exist. Now, let's examine whether when negative and positive energy exist, each of them can has charges.

$$\begin{array}{c}
 \text{Energy conservation} \\
 \left[E_T = 0 = (+E) + (-E) = \sum +m_+ c^2 + \sum -m_- c^2 + \sum +K_{+m} + \sum -K_{-m} + \sum U = 0 \right] \\
 \begin{array}{cccccc}
 \underbrace{\hspace{1.5cm}} & \underbrace{\hspace{1.5cm}} & \underbrace{\hspace{1.5cm}} & \underbrace{\hspace{1.5cm}} & \underbrace{\hspace{1.5cm}} & \underbrace{\hspace{1.5cm}} \\
 \text{Nothing} & \text{Pair Creation} & \text{Positive mass} & \text{Negative mass} & \text{Kinetic Energy} & \text{Potential Energy} \\
 & & \text{Something} & \text{Something} & &
 \end{array}
 \end{array}$$

Figure 5: Zero Energy Universe model-2. [29] Model that considers negative mass as negative energy. Simply put, negative mass indicates that energy can be locally distributed and has characteristics as particle.

1) Electrostatic self-energy U_{es}

Since the charge Q is the set of infinitesimal charge dQ , electric force is operated between infinitesimal charges and therefore, electrostatic self-energy exists due to the presence of charge Q itself.

When spherical symmetry and even distribution of charges are assumed, U_{es} , the electrostatic self-energy (or electrostatic binding energy $(-U_{es})$) is as follows:

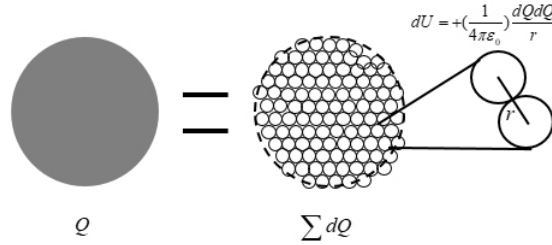


Figure 6: Since all charge Q is a set of infinitesimal charge dQ s and each dQ is electromagnetic source, too, there exists electrostatic potential energy among each of dQ s.

$$U_{es} = +\frac{3}{5} \left(\frac{1}{4\pi\epsilon_0} \frac{Q^2}{R_{es}} \right) \quad (18)$$

However, **electrostatic self-energy has positive values for both positive and negative charges.**

$$U_{es} = +\frac{3}{5} \left(\frac{1}{4\pi\epsilon_0} \frac{Q_+^2}{R_{es}} \right) = +\frac{3}{5} \left(\frac{1}{4\pi\epsilon_0} \frac{Q_-^2}{R_{es}} \right) > 0 \quad (19)$$

2) Positive energy can has charges, since a part of its positive energy or mass is able to be transformed into electrostatic self-energy of charges.

$$E_T = +E_0 = +E_0 + (-U_{es}) + (+U_{es}) = (+E_0 - U_{es}) + \frac{3}{5} \left(\frac{1}{4\pi\epsilon_0} \frac{Q^2}{R_{es}} \right) \quad (20)$$

However, **negative energy does not have positive energy to produce charges, so it is very unlikely to have charges.**

3) Limit of spontaneous process by the principle of negative mass

In positive mass, the transformation for E_0 to $E_0 - U_{es}$ is the process in which energy is lowered, which corresponds to the fundamental principle that positive mass is stable at the low energy state.

$$E_T = -E_0 = -E_0 + (-U_{es}) + (+U_{es}) = -(E_0 + U_{es}) + \frac{3}{5} \left(\frac{1}{4\pi\epsilon_0} \frac{Q^2}{R_{es}} \right) \quad (21)$$

Meanwhile, in negative mass, the transformation for $-E_0$ to $-E_0 - U_{es}$ is the process in which energy is lowered, which does not correspond to the fundamental principle that the negative mass is stable at the high energy state.

Therefore, negative mass is unlikely to have charges, according to this principle.

4) **Electrostatic self-energy has a potential to explain substantial parts of fundamental particle mass.** [30]

Most parts of fundamental particles' rest mass are likely to be originated from the electrostatic(or electromagnetic) self-energy, due to the presence of charges. Although there are many points to be additionally considered, such a model's suggestions for the magnitude of quark should be currently examined with electrostatic self-energy equivalent to mass energy.

$$E = mc^2 = \frac{3}{5} \left(\frac{1}{4\pi\epsilon_0} \frac{Q^2}{R_{es}} \right) \quad (22)$$

$$R_{es} = \frac{3}{5} \left(\frac{1}{4\pi\epsilon_0} \frac{Q^2}{mc^2} \right) \quad (23)$$

For convenience of calculation, it is defined as follows $Q = ke$, $mc^2 = \alpha(eV)$

$$R_{es} = \frac{3}{5} \left(\frac{1}{4\pi\epsilon_0} \frac{Q^2}{mc^2} \right) = \frac{3}{5} \left(\frac{1}{4\pi\epsilon_0} \right) \left(\frac{k^2 e^2}{mc^2} \right) = \frac{k^2}{\alpha} (8.64 \times 10^{-10}) [m] \quad (24)$$

If the charge is distributed only in the spherical shell, the radius is reduced by approximately 16.7%.

$$U_{es-shell} = \frac{1}{2} \left(\frac{1}{4\pi\epsilon_0} \frac{Q^2}{R_{es}} \right) \quad (25)$$

$$R_{es-shell} = \frac{1}{2} \left(\frac{1}{4\pi\epsilon_0} \frac{Q^2}{mc^2} \right) = \frac{k^2}{\alpha} (7.20 \times 10^{-10}) [m] \quad (26)$$

Since mass is $2.4MeV/c^2$ and quantity of electrical charge is $(+2/3)e$, for up quark, if $k=2/3$ and $\alpha = 2.4 \times 10^6$ are substituted,

$$R_{es-U} = \frac{k^2}{\alpha} (8.64 \times 10^{-10}) [m] = \frac{\left(\frac{2}{3}\right)^2}{2.4 \times 10^6} (8.64 \times 10^{-10}) [m] = 1.6 \times 10^{-16} m \quad (27)$$

By interpreting this, it can be inferred that the mass of up quark is derived from electrostatic self-energy, if the radius of up quark is approximately $R_{es-U} = 1.6 \times 10^{-16} m$ and here, charges are evenly distributed.

If inferences of other quarks can be acquired,

Down quark's mass: $4.8MeV/c^2$, charge: $(-1/3)e$

$$R_{es-D} = 2.0 \times 10^{-17} m \quad (28)$$

Strange quark's mass: $95MeV/c^2$, charge: $(-1/3)e$

$$R_{es-S} = 1.01 \times 10^{-18} m \quad (29)$$

Charm quark's mass: $1.275GeV/c^2$, charge: $(2/3)e$

$$R_{es-C} = 3.01 \times 10^{-19} m \quad (30)$$

Bottom quark's mass: $4.18GeV/c^2$, charge: $(-1/3)e$

$$R_{es-B} = 2.29 \times 10^{-20} m \quad (31)$$

Top quark's mass: $172.44GeV/c^2$, charge: $(2/3)e$

$$R_{es-T} = 2.22 \times 10^{-21} m \quad (32)$$

It is desirable to think that the magnitude of quark from such a simple model is smaller than that of an atomic nucleus.

The fact that the six quark radii (or diameters) vary by roughly 10^1 orders of magnitude, suggests that there is some principle or rule. We considered only the electrostatic self-energy value. Nonetheless, some rules seem to suggest that the self-energy of the charge may be the most important term.

If there is a fourth-generation quark, we can predict the mass of the fourth-generation quark by using this reasoning.

The above calculation suggests the possibility that electrostatic self-energy due to the presence of charges can explain some parts of (single) fundamental particle mass.¹ In order to make a precise model, the model related with kinetic and other energy, relativistic effects and quantum mechanics and orbital model(in case of electron) related with charge distribution can be also considered.

There are also exceptions such as electron. In the case of electron, it is estimated that other factors are important because the rest mass is too small. In the case of electron, it is presumed that the effect of increasing the distribution of the charge like the orbital model should be reflected. Even in the case of neutral particles, there are cases where there are positive and negative charges inside the particle. In the case of composite particles, the electrostatic self-energy for each charge distribution and the binding energy must be considered.

This inference also suggests that negative energy is unlikely have charges, because electrostatic self-energy is positive mass (energy), which provides an evidence about the fact that electromagnetic interaction does not occur. Hence, negative mass does not have any charges and is very unlikely to have electromagnetic interaction. In addition, even if other fundamental forces are applied to the negative mass, the fundamental charges underlying the forces may be supposed to have positive self-energy.

This corresponds to characteristics required for the dark matter, and also gives some explanations to “why does the dark matter not have electromagnetic interaction?”

3. Centripetal force effects that negative mass outside the galaxy creates inside it [18] [19]

If negative mass(energy) and positive mass(energy) were came into being together at the beginning of universe, since positive masses have attractive gravitational effects with each other, so it forms stars and galaxy. However, negative masses have repulsive gravitational effects towards each other, so it cannot form any giant structure and may spread out almost uniformly across the whole area of universe.

Owing to the effect of negative mass and positive mass, negative mass disappears near massive positive mass structures (such as the galaxy, etc.) after meeting positive mass. However, negative mass, which came into existence at the beginning of universe, can still exist in a vacuum state outside of general galaxy.

Let's examine the effect of the centripetal force of negative mass that is outside the galaxy on mass m , which is located within the galaxy.

1) If we assume that the empty space is filled with both negative mass and positive mass of the same density then,

$$\text{Total energy of the white empty space} = 0 = (+mc^2) + (-mc^2) = 0$$

2) Negative mass is now uniformly distributed over the whole area so the effect of negative mass on mass m becomes 0. (fig. b))

3) The remaining positive mass is distributed over the white area at the density of negative mass. (fig. c)) Gravity that uniformly distributes positive mass works on positive mass m located on radius r is worked upon only by the distribution of mass within radius r . -Shell Theorem.(fig. d))

¹However, this seems to deny the logic of the Higgs mechanism, which gives mass to the fundamental particles. This model claims that most of the mass of a charged particle is from the charge distribution. Electrostatic self-energy comes from the definition of electric force or electrostatic potential energy. Perhaps, is the Higgs mechanism a mechanism that only applies to weak interaction particles?

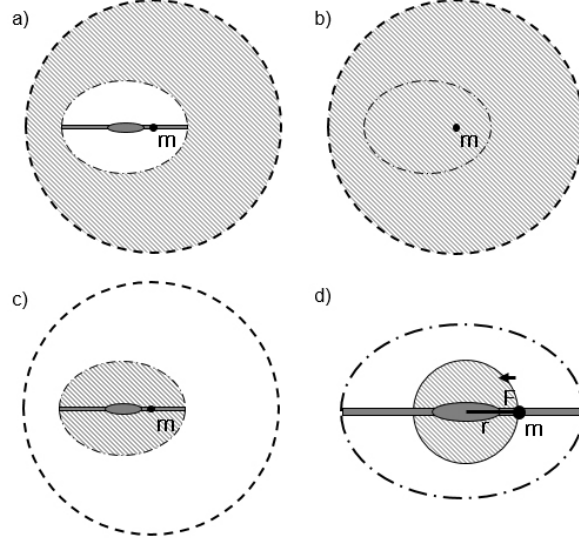


Figure 7: The structure of the galaxy surrounded by negative mass that is distributed equally.(a) The white area is the area where negative mass almost does not exist.

Therefore, the effect of negative mass that remains outside of the galaxy is compressive to the distribution of positive mass within the radius r in the galaxy. This means that the dark matter, consisting of negative mass outside galaxy, has additional effect of centripetal force on stars within the galaxy.

$$\frac{mv^2}{r} = \frac{G(M_m + M_{dm})m}{r^2} \quad (33)$$

$$v = \sqrt{\frac{G(M_m + M_{dm})}{r}} = \sqrt{\frac{G(M_m + \frac{4\pi r^3 \rho_{dm}}{3})}{r}} = \sqrt{(GM_m)\frac{1}{r} + (\frac{4\pi G \rho_-}{3})r^2} \quad (34)$$

This effect suggests that the further from the center of the galaxy, the more mass effect exists and agrees with the current situation where the further from the center of the galaxy, the more dark matter exists.

Consider a thin uniform circular ring of radius a and negative mass M . A test mass m is placed in the plane of the ring.

If $r \ll a$

$$F_{dm} = \frac{1}{2} \frac{GM_{dm}mr}{a^3} = \frac{1}{2} \frac{G(2\pi a(-\rho_-))mr}{a^3} = -\frac{G\pi\rho_-mr}{a^2} \quad (35)$$

$$v = \sqrt{\frac{GM_m}{r} + \frac{GM_{dm}r^2}{2a^3}} = \sqrt{(GM_m)\frac{1}{r} + (G\pi\rho_-)\frac{r^2}{a^2}} \quad (36)$$

If dark matter is exist in the galaxy, dark matter will be affected by the distribution of stars and interstellar gas in the galaxy. That is, the density of dark matter around the solar system will be higher than the average of the galaxy. The existing CDM model suggests that there is a local distribution of dark matter around the local gravitational source (such as solar system). Some models offer a theoretical background on how dark matter is not detected in the solar system by lowering the total amount of dark matter around the solar system by assuming that dark matter is completely evenly distributed in the galaxy.

This model explains the presence of additional gravitational effects in the galaxy and the reason why the dark matter is not found on the earth or in the vicinity of the solar system. **In this model, dark matter**

(negative mass) exists outside the galaxy, and there is only a gravitational effect in the galaxy that is not affected by the local gravitational source (such as solar system) in the galaxy.

We observed only the effect of matter in the Earth. However, it is presumed that the observation of the gravitational effect of dark matter and dark energy at the galactic scale or above, is due to the existence of negative energy and negative mass outside the galactic structure.

4) The model above is a principle explanation. We assumed a uniform distribution for simple calculations, but in reality, the density of negative mass is higher as it is closer to galaxy or galaxy cluster, and is lower as it is farther. Moreover, axisymmetric distribution due to rotation of the galaxy should be also considered. It is also possible to consider repulsive force affected by negative mass as well as negative mass's free fall onto the center of the galaxy.

5) Computer simulation [20]
<https://youtu.be/MZtS7cBMic4?t=364>

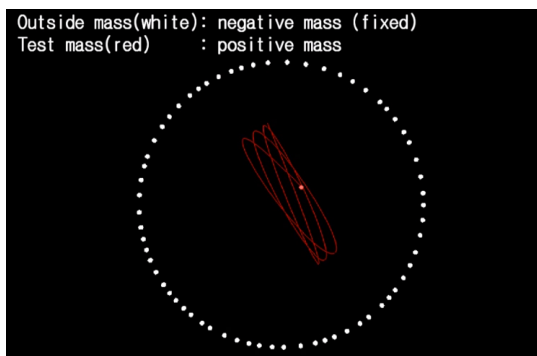


Figure 8: White : negative mass(fixed), Red : positive mass(free). The positive mass vibrates.

If the negative mass is disposed at the outline, the positive mass vibrates. Therefore a kind of centripetal force exists. This corresponds to the “centripetal force” when considering rotation of the galaxy.

4. Low interaction between dark matters: occurring from repulsive gravitational effects between dark matters

The existing CDM models argue that dark matters are almost evenly distributed as they only have gravitational interaction, except for electromagnetic one, even though dark matters are five times or hundreds times more than other masses. [11] [25] However, is this process true?

There are more certain explanations and rules in the model of negative mass.

Positive masses have attractive gravitational effects with each other, so it forms stars and galaxy. However, negative masses have repulsive gravitational effects towards each other, so it cannot form any giant structure and may spread out almost uniformly across the whole area of universe. Also, negative mass exists outside the galaxy, and there is only a gravitational effect inside the galaxy.

This provides strong explanations to the phenomenon that current dark matters do not strongly interact with each other, but are almost evenly distributed.

5. Negative mass can also explain dark energy. [18] [19] [27]

Negative mass engenders antigravity which is consistent with effects of dark energy that allows for accelerating expansion of the universe.

Friedman equation can be induced from 00 component of field equations. But we can also induce this from conservation of energy in classical mechanics, which helps capture the situation definitely. [25]

What we are looking for in cosmology is one attraction term and one repulsion term. If a negative mass exists, we can get it.

$$E = T + V = \frac{1}{2}mv^2 - \frac{GMm}{r} - \frac{1}{6}\Lambda mc^2 r^2 = \text{const.}$$

$$v = \frac{dr}{dt} = Hr = HR\varpi$$

$$\frac{1}{2}m\varpi^2 \left[\left(\frac{1}{R} \frac{dR}{dt} \right)^2 - \frac{8\pi G\rho}{3} - \frac{1}{3}\Lambda c^2 \right] R^2 = \frac{1}{2}m\varpi^2 [-kc^2]$$

Figure 9: The Friedmann equation can derive from field equation or mechanical energy conservation equation.

If negative mass and positive mass coexist, gravitational potential energy consists of the following three items.

$$U_T = \sum_{i<j} \left(-\frac{Gm_{+i}m_{+j}}{r_{++ij}} \right) + \sum_{i<j} \left(-\frac{G(-m_{-i})(-m_{-j})}{r_{--ij}} \right) + \sum_{i,j} \left(-\frac{G(-m_{-i})m_{+j}}{r_{-+ij}} \right) \quad (37)$$

$$U_T = \sum_{i<j} \left(-\frac{Gm_{+i}m_{+j}}{r_{++ij}} \right) + \sum_{i<j} \left(-\frac{Gm_{-i}m_{-j}}{r_{--ij}} \right) + \sum_{i,j} \left(+\frac{Gm_{-i}m_{+j}}{r_{-+ij}} \right) \quad (38)$$

$$U_T = U_{++} + U_{--} + U_{-+} \quad (39)$$

U_{--} is attractive term and U_{-+} is repulsive term.

The present cosmological constant can be obtained by adding potential energy $U_\Lambda = -\frac{1}{6}\Lambda mc^2 r^2$ to mechanical energy conservation equation. [25]

If we insert “new potential energy term” into mechanical energy conservation equation, we will get a dark matter term and dark energy term. And if U_{++} , U_{--} , U_{-+} has a ratio(4.9% : 26.8% : 68.3%) between each other, maybe, we will estimate that ratio of energy density such as 4.9% : 26.8% : 68.3% exist. [19]

This model can prove the energy composition(Matter : Dark matter : Dark energy) ratio of the universe and CCC (Cosmological Constant Coincident) Problem. [19]

Roughly calculation :

Average of WMAP and Planck - Matter : Dark Matter : Dark Energy = 4.75% : 25.05% : 70.20%

Average of Pair Creation Model - Matter : Dark Matter : Dark Energy = 4.75% : 25.00% : 70.25%

6. Gravitational lens effect by negative mass [18]

Generally, it is possible to examine the existence of dark matter with the existence of additional mass with the effect of gravitational lensing. If negative mass is dark matter, so if we try to examine the effect of gravitational lensing, previously the gravity between positive mass is attraction, so it has the shape of convex lens to collect within the form, whereas the force between negative mass and positive mass is repulsion, so a set of massive negative mass can make the effect that distorts observation target in the form of concave lens.

In order to observe gravitational lens effects due to negative mass in the universe, the negative mass should independently constitute large mass. However, it is not possible, since the negative masses have repulsive gravitational interaction with each other. Therefore, it is difficult for us to observe gravitational lens effects independently caused by negative mass. However, there are spaces in which negative masses are concentrated, in the universe. They are in the vicinity of the galaxy or the cluster of galaxies, which consist of positive masses, because of attractive gravitational effects of large positive mass on negative mass.

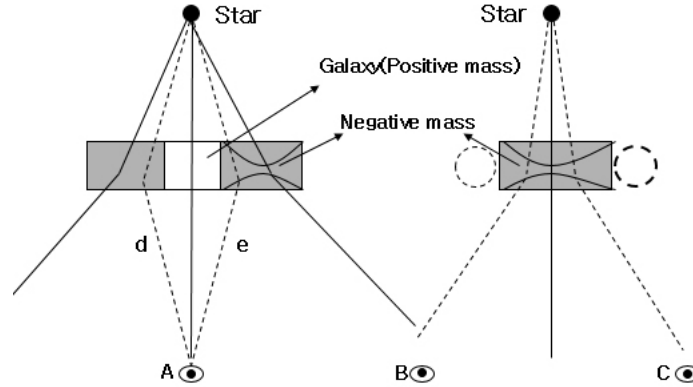


Figure 10: Concave Gravitational lensing effect. The left side is the Gravitational lensing effect that occurs when the galaxy is surrounded by negative mass. The right side is Gravitational lensing effect that occurs when negative mass exists alone

But in the model of dark matter with negative mass in this study, negative mass is distributed out of galaxy, not within galaxy. Therefore, the effect of concave gravitational lensing by negative mass out of galaxy will be presented to an observer on the earth in the same form as the effect of convex gravitational lensing which galaxy works.

For the situation presented on the left when observing the light on the earth which passed through galaxy surrounded with negative mass, this study suggested that there is invisible dark matter in galaxy, and owing to this gravity it can be happened owing to the effect of convex lens, it means, if there is any matter on the left and right side of galaxy that plays a role of concave lens, it is difficult to classify convex lens and its form.

If we consider the situation that we can observe purely the effect of concave gravitational lensing, that situation is just the same as the situation when there is single concave lens on the right in figure.

First, an observer on the earth must observe it on Position B and C after moving by considerably great distance as compared with the size of galaxy, but the earth has never changed the position of observation from the target for distant observation.

Second, real observation on the earth is the single B or C situation in Figure on the right, and if an observer on the earth performed observation previously on C, generally an observer of C would describe the effect of gravitational lensing is generated because there is invisible dark matter on the right of black and white area(circle drawn with dotted line on the right).

Anyway, it is possible that gravitational lens effects by negative mass are similar with those by positive mass. However, according to this model, the formula for gravitational lens based on the existing positive mass may be accurate for the scale of each fixed star, but inaccurate for the scale more than the galaxy.

7. Other characteristics related with dark matter

1) Dark matter is required by rotation curve of the galaxy. However, why is it not detected on the earth or the solar system?

According to negative mass model, negative mass exists outside the galaxy, while additionally exerting centripetal force effects inside the galaxy, so it cannot be observed in the vicinity of the earth. Dark matter (negative mass) exists outside the galaxy, and there is only a gravitational effect in the galaxy.

2) Why is negative mass not detected in LHC?

Broken particles also only produce particles with positive energy, since the experiment is conducted only with positive energy particle.

3) Negative mass satisfies the condition that requires dark matter be particles outside the Standard Model.

4) Lower interaction between dark matters and almost even distribution: occurring from repulsive gravitational effects between negative masses.

5) Peculiar phenomenon where dark matter is observed to be separated with the galaxy, galaxies with little dark matter [31]

Negative mass can be separated with the galaxy, in this model. For example, this phenomenon can occur, if nearby galaxies attract much of negative mass.

6) Although negative mass may undergo pair-annihilation by colliding with positive mass, this process can be limited by other physical laws.

For example, consider the charge conservation law. When a positive mass with charge collides with negative mass, they may undergo pair annihilation, from the perspective of energy. However, if an electron (or positive energy) disappears, where should charge go? In that case, the conservation law of electrical charge may be invalid. If the conservation law of electrical charge should be held, such a pair-annihilation may be prohibited. In other words, **the pair-annihilation is unlikely to occur even when negative mass meets positive mass.** Thus, negative masses may exist inside galaxies.

Negative mass essentially satisfies many characteristics of dark matter, without introducing a separate assumption. It is necessary to seriously examine the negative mass model just because negative mass is required by the law of conservation of energy and can explain accelerating expansion of the universe.

Way to go!

Newton and Einstein already died, but we live now!, though sometimes we feel sorrow.

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