## Using metaballs to model the pre-ringdown phase of the merger of Schwarzschild black holes

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## Abstract

In this paper, Blinn's metaballs are used to model the pre-ringdown phase of the merger of Schwarzschild black holes.

## 1 Metaballs

Metaballs have been used in computer graphics ever since their discovery by Jim Blinn [1]. They were originally used to visualize electron density. In this paper we will model Schwarzschild black holes using metaballs.

Where  $G = c = \hbar = k = 1$ , there is an analytical solution for the pre-ringdown phase of the merger of n = 2 Schwarzschild black holes travelling directly toward each other:

$$f(l) = \sum_{i=1}^{n} \frac{2M_i}{r_i}.$$
 (1)

Here  $M_i$  is the mass of the *i*th black hole, and

$$r_i = \sqrt{(l.x - v_i.x)^2 + (l.y - v_i.y)^2 + (l.z - v_i.z)^2},$$
(2)

where l is the sample location, and  $v_i$  is the centre of the *i*th black hole. The event horizon is given by

$$f(l) = 1. \tag{3}$$

Included are figures of the pre-ringdown phase of Schwarzschild black hole mergers. The event horizon was tessellated using the Marching Cubes algorithm [2]. Analogously, we are visualizing graviton density.

The C++ code for this paper can be found at [3].

Another method for generating the event horizon is given in [4].

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Figure 1: Two black holes of unit mass each, at a distance of 11.



Figure 2: Two black holes of unit mass each, at a distance of 10.



Figure 3: Two black holes of unit mass each, at a distance of 9.



Figure 4: Two black holes of unit mass each, at a distance of 8.



Figure 5: Two black holes of unit mass each, at a distance of 7.



Figure 6: Two black holes of unit mass each, at a distance of 6.



Figure 7: Two black holes of unit mass each, at a distance of 5.



Figure 8: Two black holes of unit mass each, at a distance of 4.



Figure 9: Two black holes of unit mass each, at a distance of 3.



Figure 10: Two black holes of unit mass each, at a distance of 2.



Figure 11: Two black holes of unit mass each, at a distance of 1.



Figure 12: *One* black hole of mass = 2.

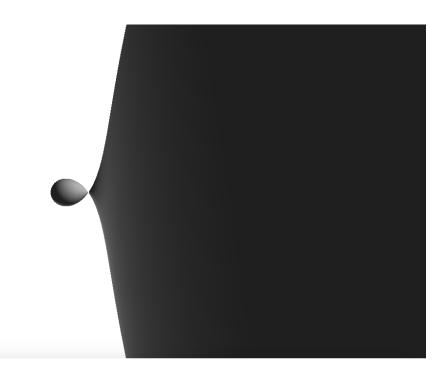


Figure 13: A unit mass black hole merging with a black hole of mass = 1000.

## References

- Blinn J. A generalization of algebraic surface drawing ACM Transactions on Graphics, Vol. 1, No. 3 (1982)
- [2] Lorensen W, Cline H. Marching Cubes: A high resolution 3D surface construction algorithm Computer Graphics, Vol. 21, No. 4 (1987)
- [3] Halayka, S. C++ code (2017) https://github.com/sjhalayka/bhmerger
- [4] Emparan R, Martinez M. Exact event horizon of a black hole merger (2016) arXiv:1603.00712 [gr-qc]