

# A New Solution to Einstein's Relativistic Mass Challenge Based on Maximum Frequency

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## Abstract

In 1905, Einstein presented his famous relativistic mass energy equation  $\frac{mc^2}{\sqrt{1-\frac{v^2}{c^2}}}$ . When  $v$  approaches  $c$ , the expression containing the moving mass approaches infinity. Einstein interpreted this in the following way: since one needs an infinite amount of energy to accelerate even a small mass to the speed of light, it would appear that no mass can ever reach the speed of light. In this paper, we present a new solution to the infinite mass challenge based on combining special relativity with insights from Max Planck and maximum frequency. By doing this we show that there is an exact limit on the speed  $v$  in the Einstein formula. This limit is only dependent on the Planck length and the reduced Compton wavelength of the mass in question.

**Key words:** Relativistic mass, maximum frequency, maximum speed, Planck length, Planck mass, relativistic Doppler shift.

## 1 A Maximum Frequency and a Maximum Velocity for Mass?

Einstein [1, 2] gave the following relativistic energy mass formula:

$$E = \frac{mc^2}{\sqrt{1-\frac{v^2}{c^2}}}. \quad (1)$$

Further, Einstein commented on his own formula

*This expression approaches infinity as the velocity  $v$  approaches the velocity of light  $c$ . The velocity must therefore always remain less than  $c$ , however great may be the energies used to produce the acceleration<sup>1</sup>*

Einstein's argument is that the mass will become infinite as  $v$  approaches  $c$  and this means that we would need an infinite amount of energy to accelerate even an electron to the speed of light. Here we will combine Einstein's special relativity with insight from Max Planck [3, 4] and show that there is another possible solution to the infinite mass challenge. The relativistic mass relationship can be derived from a two-sided Einstein relativistic Doppler shift. Assume a mass is sending out two energy beams. These beams have a frequency of  $f_{ab}$  and  $f_{ba}$  as observed from the mass sending them out, and further  $f_{ab} = f_{ba}$  as observed from this frame. From another frame moving at speed  $v$  relative to this mass, based on the relativistic Doppler shift one will observe these frequencies to be

$$\hat{f}_a = f_a \frac{(1 - \frac{v}{c})}{\sqrt{1 - \frac{v^2}{c^2}}} \quad (2)$$

and

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<sup>1</sup>This quote is taken from page 53 in the 1931 edition of Einstein's book *Relativity: The Special and General Theory*. English translation version of Einstein's book by Robert W. Lawson.





become Planck masses just before reaching the speed of light and then they will burst into pure energy traveling at the speed of light.

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